Physiological Time Series: Analyse and Remove the Drift in 1-2-3

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Abstract

A precondition for developing diagnostic tools based on analysing physiological time series is that there is pattern, i.e. information, in the data. Systematic variation in the data set is often masked by baseline drift and physiological fluctuations. In this study a simplest possible algorithm to eliminate the effect of drift and detect short-term pattern in physiological data is presented. The time series, \( x_i \), is filtered for the occurrences of three consecutive points with different values (\( x_i \neq x_{i+1} \neq x_{i+2} \)). Six different patterns are identified. The probability distribution of the pattern suggests if the time series is random or generated from a possible goal directed regulating activity. If the information entropy of the probability distribution of the pattern is close to one (not infinite long time series), the time series most likely come from a underlying process not offering qualitative information suitable for diagnostic purposes.

The method is demonstrated on a data sequence generated from the logistic map in the infinite periodicity condition and a recorded optokinetic nystagmus amplitude time series.

Keywords

Physiological time series; Drift; Symbolic dynamics; Information pattern

Introduction

When analysing physiological data for information pattern, we often face the problem of drift and physiological fluctuations [1].

In this study the consecutive running three data point pattern, with different values \((x_i \neq x_{i+1} \neq x_{i+2})\) in a time series is analysed. Six different patterns are identified. The probability distribution of the pattern from a random time series will be approximately flat, i.e. equally many samples of each pattern (the distribution from an eternally long random time series will be totally flat).

The algorithm is tested on a sequence from the chaotic regime of the logistic map with infinite periodicity,

\[ x_{i+1} = r x_i (1-x_i) \quad r=3.8 \]

and an optokinetic nystagmus amplitude (OKNA) time series [2-4]. Optokinetic nystagmus is the eye movement reflex elicited by the tracking of a moving field.

Methods

For the purpose of removing drift and testing for short-term information pattern in the time series data the following procedure was applied.

From the time series \( x_i \), find the three points data series \( w_i \), where \( w_i \) is

\[
\begin{pmatrix}
123: (x_i < x_{i+1} < x_{i+2}) \\
132: (x_i < x_{i+2} < x_{i+1}) \\
213: (x_{i+1} < x_i < x_{i+2}) \\
231: (x_{i+2} < x_{i+1} < x_i) \\
312: (x_{i+2} < x_{i+1} < x_i) \\
321: (x_{i+1} < x_{i+2} < x_i)
\end{pmatrix}
\]

\]

Compute the probability density distribution \( p_k \),

\[
\sum_{k=1}^{b} p_k = 1, \text{ where bins} = \{123, 132, 213, 231, 312, 321\}
\]

Calculate the normalized information entropy, \( I \), of the probability distribution [3,4,5]

\[
I = -\frac{1}{\log(6)} \sum_{k=1}^{b} p_k \log(p_k), \quad 0 \leq I \leq 1
\]

Results

Figure 1 shows the probability distribution, \( p_k \), of the three points data pattern series, \( w_i \), for a) logistic map, b) the logistic map with linear added drift of two times the standard deviation (SD) (\( n=1000 \)) and for c) OKNA time series without and d) with linear added drift of two times the SD (\( n=338 \)). The unequal distribution of the probability distribution shows that some patterns occur more often than others, which indicates information in the data sets. We can see that adding 2*SD drift does not change the pattern distribution or the calculated information entropy, even for the short OKNA time series. The entropy of the pattern distribution for the logistic map without and with added 2*SD drift was calculated to \( I_{\text{logmap}}=0.84 \) and \( I_{\text{OKNA}}=0.98 \) for the OKNA time series.

Discussion and Conclusion

The purpose of this study was to test out a simplest possible algorithm to eliminate the effect of drift and detect short-term pattern in physiological data. It has been shown that the method is robust against drifting noise. Adding linear drift of 2*SD did not change the pattern distribution, or the calculated information entropy, for the logistic map or the short OKNA time series.

It remains to see if qualitative information in physiological time series [5] reflects some dynamical properties in the underlying physiological regulating mechanism, that can be detected by this method and substantiate it’s use for diagnostic purposes.
Figure 1: Upper (a) right diagram shows the probability distribution of the three points data pattern series with different values \( x_i \neq x_{i+1} \neq x_{i+2} \) in the logistic map series (left), and the diagram under (b) right for the logistic map with linear added drift of two times the standard deviation (left). (c) Shows the three points data pattern distribution (right) for the OKNA time series (left), and (d) (right) for the OKNA time series with linear added drift of two times the standard deviation (left). The calculated normalized information entropy is the same for pattern distribution for logistic map with and without added drift, and for the OKNA time series with and without added drift.

References


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