



Research Article

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Design of Nonlinear Kerr Lens (NKL) and Method of Implementation of All Optical Logic Gates and Processors using a Single NKL

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Abstract

A design of nonlinear lens using Kerr effect is described. The incident light changes the focal length of the lens and this light induced focal length change are utilized to optical switching and routing. Using this type of lens all optical 3 input AND, X-OR and majority function logic gates, two input AND, X-OR, NAND, NOR, X-NOR, optical processors half Adder, Full Adder are implemented. Controlled operation of the logic gates is also explained.

Keywords

Kerr effect; Optical switching; Optical logic gate; Optical logic processors

Introduction

Optics has established itself as a promising candidate for future parallel computation and communication system. All optical switching has an important role for implementation of the optical computation and communication system components. There are several types of switching techniques based on different kind of optical phenomena and materials. Nonlinear material based switching is very important for the application in optical switching technology. Different nonlinear phenomena in Semiconductor optical amplifier (SOA) [1], periodically poled lithium niobate (PPLN) [2], high nonlinear fiber (HNLF) [3], difference frequency generation (DFG) [4], Second harmonic generation (SHG) with optical parametric amplification (OPA) [5], nonlinear prism based on refraction [6], total internal reflection prism [7-9], nonlinear-linear slab (NL-L) [10,11], etc are utilized to design optical logic gates and processors by various researchers. SOA based devices require proper biasing current for its operation, PPLN has the disadvantages of having temperature and polarization sensitiveness, DFG and parametric process are very difficult to be implemented and requires high power lasers. The HNLF require a large length to show considerable effect, otherwise very popular nonlinear device and total reflectional prisms require high power for its operation. In contrast, nonlinear prism and NL-L slab based devices are very effective having no such drawbacks [6,10,11], which are based on optical Kerr effect. The effectiveness of the switching depends on the amount of deviations

produced by the nonlinearity of the devices (materials) and is better for prism shaped devices compared to slab structure [6] and devices based on absorption are less susceptible to optical damage and has less speed of operation compared to refraction based devices which will be proposed in this communication. However, the deviation produced by a prism depends on the angle of incidence, and very small deviations can be produced for high intensity. Comparatively a lens can produce more deviation with same intensity and its focal length does not depend on the angle of incidence but is a constant quantity for a particular lens material and surroundings. It depends on the radii of curvature of the curved surfaces and can be adjusted to make the focal lengths as desired. In this communication a nonlinear lens utilizing Kerr effect in nonlinear materials. The variation of focal length, variation of Change of focal length, angular deviation corresponding to focal length with intensity of the incident light is analyzed. The all-optical switching based on the NKL is utilized to design logic gates and processors like three input AND, X-OR and majority function logic gates, two input AND, X-OR, NAND, NOR, X-NOR, optical half Adder, full Adder. The devices based on NKL are cascade-able, and higher order logic processors can be implemented using this in future.

Theory of Optical Switching and Design of Nonlinear Kerr Lens (NKL)

The refractive index of many optical materials depends on the intensity of the light, and is called Kerr effect, by analogy with the traditional Kerr electro optic effect [12]. This effect can be explained by nonlinear polarization and the intensity dependent refractive index is given by

$$n = n_0 + n_2 I \quad (2.1)$$

Here I represents the intensity of the incident light, n_0 represents the usual weak field refractive index, and n_2 is the nonlinear correction term. The nonlinear change may be produced by several mechanisms such as electronic polarization, molecular orientation change, thermal effects, photo-refraction etc. Electronic polarization produces n_2 with response time of femto-seconds and thus very fast.

This refractive index change is utilized to change direction of propagation of a light beam of suitable intensity and optical switching can be achieved. In a nonlinear medium, this refractive index change produces several effects like self focusing, self trapping, phase conjugation, optical bi-stability etc may be useful for optical logic processors and memory devices. Few important nonlinear materials with values of linear and nonlinear refractive indices are listed below [12]. Table 1 shows that some polydiacetylenes (PTS) shows n_2

Table 1: Some materials and their nonlinear refractive indices.

Nonlinear Materials	n_0	n_2 in m^2/W at wavelength in μm
Al_2O_3	1.8	2.9×10^{-20} at 1 μm
CdS	2.34	5.1×10^{-18} at 1 μm
Fused Silica	1.47	3.2×10^{-20} at 1 μm
CS_2	1.63	3.2×10^{-18} at 1 μm
PTS	-	3×10^{-16}
CS-3-68 glass	-	2.3×10^{-14} at 3 μm
ZnSe	2.7	3×10^{-18} at 1 μm

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hundred times that of CS_2 and a special type of glass CS-3-68 glass nano-particles shows n_2 ten thousand times that of CS_2 and ZnSe. So these materials will find potential applications in future for all optical processing. In the work [6], nonlinear prism based on CS_2 is designed and analyzed. In this communication, CS_2 is used to design the device NKL. A single NKL based module has the capability of giving simultaneously several outputs of all optical 3 input AND, X-OR and majority function logic gates, two input AND, X-OR, NAND, NOR, X-NOR, optical processors like half Adder and Full Adder reducing highly the design complexity and enabling integration capability.

The optical switching in this communication is utilized by designing a nonlinear lens based on Kerr effect defined by Equation 2.1 and the device is called nonlinear Kerr lens(NKL in short). In the Figure 1 the lens is shown.

As we know the focal length, f of a lens is given by Lens Makers' formulae [13],

$$\frac{1}{f} = (n-1) \left(\frac{1}{r_1} - \frac{1}{r_2} \right) \quad (2.2)$$

Where r_1 and r_2 are the radii of curvatures of the two surfaces of the lens and n is the refractive index of the material of the lens. If we consider biconvex lens and take $r_1=r=-r_2$, the Equation 2.2 gives focal length as

$$\frac{1}{f} = (n-1) \left(\frac{2}{r} \right) \quad (2.3)$$

If the refractive index is intensity dependent as given in Equation 2.1, then the focal length will also be dependent on the intensity of the incident light. Thus, the intensity dependent focal length of the lens can be written as (using Equation 2.1 in 2.3)

$$f_I = 2r / (n_0 - 1 + n_2 I) \quad (2.4)$$

Now when the incident light intensity $I=0$, the focal length becomes

$$f_0 = 2r / (n_0 - 1) \quad (2.5)$$

Equations 2.4 and 2.5 show that $f_I < f_0$, so the direction of propagation will be changed (Figure 1). If light of intensity $>I$ is incident, the focal length becomes smaller and this can be utilized for all optical switching. The change in focal length is given by

$$\Delta f = \frac{rn_2}{2(n_0-1)[(n_0-1)+n_2 I]} \quad (2.6)$$

The angular deviations are calculated from the relation

$$\Delta\theta = \frac{\Delta f}{f} \frac{180}{\pi} = \frac{n_2}{(n_0-1)+n_2 I} I \frac{180}{\pi} \quad (2.7)$$

It is interesting to note that, the angular deviations are independent of the geometry of the lens but depend on the intensity of the incident light only.

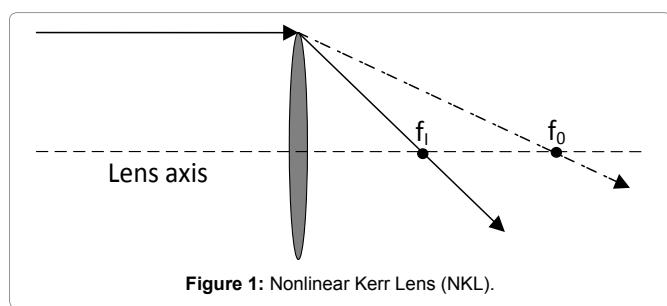


Figure 1: Nonlinear Kerr Lens (NKL).

Analysis of the Switching of NKL

To analyze the switching of the NKL designed in the section 2 above we consider radius of curvature r equal to 1m, and parameters of CS_2 given in the Table 1, i.e. $n_0 = 1.63$, $n_2 = 3.2 \times 10^{-18} \text{ m}^2/\text{W}$. With these parameters the focal length without light becomes $f_0 = 0.79 \text{ m}$. The variation of focal length with the intensity of light is shown in the Figure 2. From Figure 2, it is clear that the focal length changes from 0.79 m to 0.70 m for an incident light of intensity $2 \times 10^{16} \text{ w/sqm}$, a change of 13% approximately.

In the Figure 3, the change in focal length is plotted against intensity of the incident light. For small intensities, the variation is almost linear. This property signifies the fact that if intensity doubles the change in focal length also doubles and very suitable for switching the light signals in different paths. This is also confirmed by the angular deviation produced by the lens as shown in the Figure 4. So for lower intensities better performance can be achievable. The nonlinear lens compared to nonlinear slab [6] obtains a greater angular deviation 47 degrees. Therefore, a lens shows better performance compared slab.

From the above analysis, it is clear that considerable change in focal length and angular deviation is achieved with light intensity of the order of 10^{16} w/sqm .

Implementation of Different all Optical Logic Gates and Logic Processors

A single nonlinear Kerr Lens (NKL) designed above is used to implement different logic gates and processors in a single module. The module is shown in the Figure 5. Here A, B, and C are three inputs,

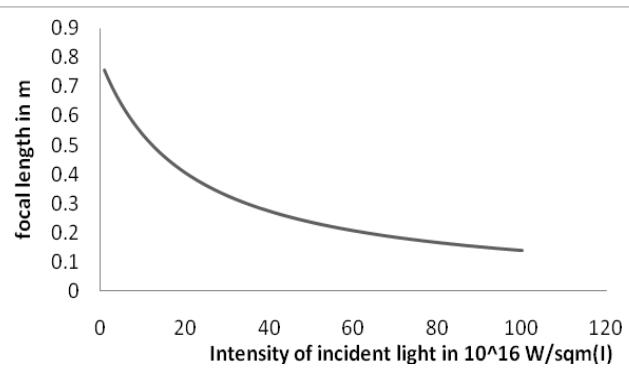


Figure 2: Variation of focal length with intensity.

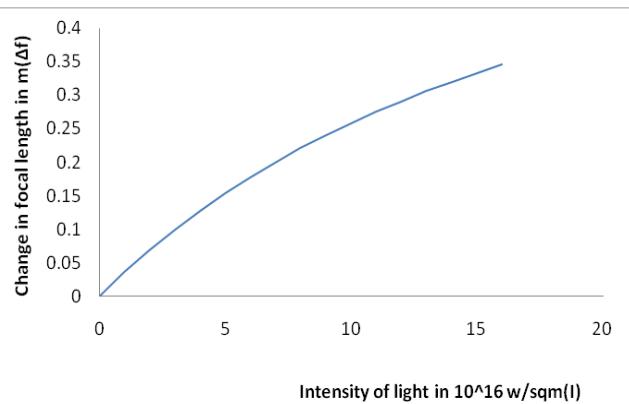


Figure 3: Variation of change in focal length with intensity of light.

combined and made incident in the nonlinear lens, P. Depending on the number of inputs the optical signals are routed to different paths PO_1 , PO_2 and PO_3 . When only a single optical signal is present the light is routed along PO_1 , when any two of the input signals A, B and C are present, the optical signal is routed along PO_2 and when

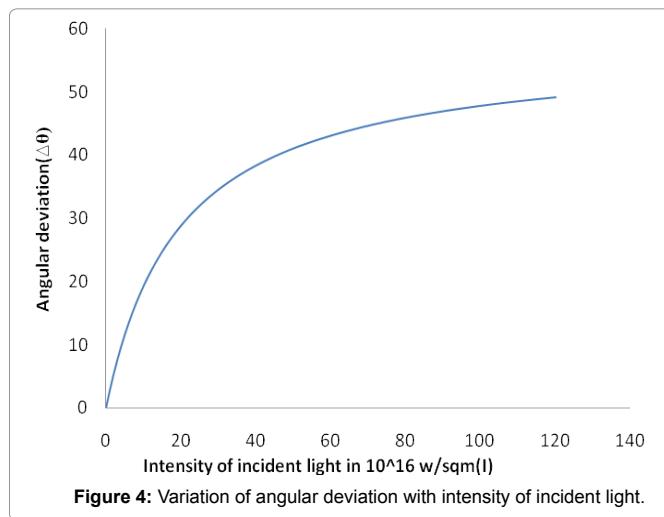


Figure 4: Variation of angular deviation with intensity of incident light.

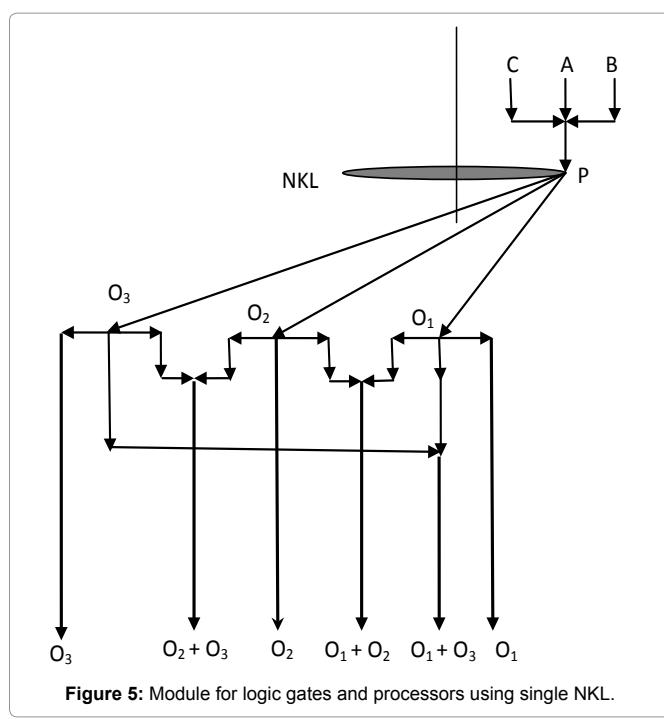


Figure 5: Module for logic gates and processors using single NKL.

all three inputs are present simultaneously, the light is routed along PO_3 . These three different paths are further combined to generate six overall outputs to generate different logic gates and logic processors. In the Table 2, inputs and different output conditions are given. From the table it is clear that if we consider the input C as control, we can generate AND, NOR, NAND, X-OR and X-NOR gates with A and B as input and if we consider three input cases then 3-input AND, 3-input X-OR and 3-input majority function can be designed as explained below with reference to Figure 5.

Two input AND gate

If we consider input C as control and set C=0, i.e. no light signal is present, the output O_2 is the operation A AND B as clear from the Table 2. Let us explain the operation of the logic gate AND.

When C = 0, four different conditions are possible.

A=0, B=0. In this condition, no signal is present in any of the output and hence the output O_2 is zero.

A=0, B=1. In this condition since only a single input is present, the light will travel along the path PO_2 of Figure 5 making output O_2 high, i.e. 1.

A=1, B=0. In this condition also only a single input is present. Hence the light will travel along the path PO_2 of Figure 5 making output O_2 high, i.e. 1 again.

A=1, B=1. Since both inputs are high, the light will travel along the path PO_3 , so there is no output in O_2 , giving low state.

So the module behaves like a two input AND gate. Again $O_2 + O_3$ is also gives A AND B operation.

Two input X-OR gate: When C=0, the output O_1 is X-OR operation of A and B. In this situation four different input conditions are possible.

A =0, B=0, no signal is present in any of the output. So O_1 is also zero (0).

A=0, B=1, signal is present in the output O_1 as the light travels along the path PO_1 giving high output.

A=1, B=0. In this condition also, the output is present at O_1 .

A=1, B=1, the light signal travels along the path PO_2 , giving no output at O_1 . So the output is zero again.

So when C=0, the output O_1 generates X-OR operation of A and B. It is interesting to note that $O_1 + O_3$ is also generates X-OR operation of A and B.

Two input NOR gate: To get operation of a two input NOR gate, we have to make C = 1, i.e. high. In this situation, the output O_1 gives

Table 2: Inputs and outputs conditions of the module of Figure 5.

INPUTS			OUTPUTS					
C	A	B	O_1	O_2	O_3	O_1+O_2	O_1+O_3	O_2+O_3
0	0	0	0	0	0	0	0	0
0	0	1	1	0	0	1	1	0
0	1	0	1	0	0	1	1	0
0	1	1	0	1	0	1	0	1
1	0	0	1	0	0	1	1	0
1	0	1	0	1	0	1	0	1
1	1	0	0	1	0	1	0	1
1	1	1	0	0	1	0	1	1

the operation of NOR gate as clear from the Table 2. Let us consider the four different cases:

A=0, B=0. In this condition, only one input signal(C in this case) is high, so the light will follow the path PO₁ giving a high (1) output.

A = 0, B=1, so that two inputs(taking C also) are high and the light signal follows the path PO₂, so that output O₁ is low i.e. zero(0).

A=1, B=0, so that again two inputs are high such that the light ray travels along PO₂, so that output O₁ is again low(0).

A=1, B=1, in this condition all the three inputs are high and the light travels along the path PO₃ from the lens, NKL.

Two input X-OR gate: When C=1, the output O₂ gives the operation of X-OR gate between A and B and is clear from the Table 2. This can be explained considering the following cases:

A = 0, B=0, only one input signal is present, so output O₂ is zero (0).

A=0, B=1, two input signals are present and hence the output O₂ is high as the light travels along the path PO₂.

A=1, B=0. In this condition also, the output is present at O₂ due to two high inputs A and C.

A=1, B=1, the light signal travels along the path PO₃, giving no output at O₂. So the output is zero again.

It is interesting to note that we can generate X-OR gate for c=0 and C=1 from different outputs.

Two input AND gate: When C=1, the output O₃ gives AND between A and B. In this condition four different cases occur. When:

A=0, B=0, only one input C is high sending light along PO₁ so that no signal in the output O₃, i.e. 0 output.

A=0, B=1.

A=1, B=0, in these conditions two inputs are high routing the light along PO₂, and no output at O₂.

A=1, B=1, in this condition all the three inputs A, B, and C are high and the light travels along PO₃, so the output O₃ is high.

This is nothing but the A and B operation when C=1. It is interesting to note that output O₂ is AND gate output when C=0.

Two input NAND gate: In the condition C=1, the output combination O₁ + O₂ is nothing but X-NOR of A and B as clear from the Table 2. There are four different conditions:

A=0, B=0, so only one input signal C is high (1) and the light travels along the path PO₁ making O₁ + O₂ high, i.e. 1.

A=0, B=1, so two inputs B and C are high sending light along the path PO₂ making O₁ + O₂ high again.

A=1, B=0, so again two inputs A and C are high making O₁ + O₂ high as light from the lens travels along PO₂.

A=1, B=1, so that all three inputs A, B and C are high routing the light along PO₃. This makes O₁ + O₂ low as no light along PO₁ and PO₂.

Two input X-NOR gate: When C=1, the combination O₁ + O₃ generates A X-NOR B operation and can be explained in the following way.

A=0, B=0 , only one input C is high sending light along PO₁ so that sending light signal to the output O₃ and making O₁ + O₃ high.

A=0, B=1.

A=1, B=0, in these conditions two inputs are high routing the light along PO₂, and no output at O₁ and O₃. So the output O₁ + O₃ is low (0).

A=1, B=1, in this condition all the three inputs A, B, and C are high and the light travels along PO₃, so the output O₁ + O₃ is high.

This is nothing but the A X-NOR B operation when C=1.

Three input AND gate: From the table it is clear that if we consider the output O₃, it will give AND operation of three inputs A, B and C. If any one of the three inputs A, B, and C is low, there will be now output in the path PO₃, making output O₃ low, i.e. zeros (0). The output O₃ is high only when all the three inputs are high because in this condition only the light propagates along PO₃ from the lens, NKL. This is nothing but the AND operation of A, B and C.

Three input X-OR gate: The output combination O₁ + O₃ gives three input X-OR operation of A, B and C. There are eight different cases.

A=0, B=0, C=0. Since all the inputs are low, no light in any of the output making O₁ + O₃ low.

A=0, B=0, C=1.

A=0, B=1, C=0.

A=1, B=0, C=0, in these three conditions only one input is high. So light will travel along PO₁, making the output O₁ + O₃ high.

A=0, B=1, C=1.

A=1, B=0, C=1.

A=1, B=1, C=0, in these three conditions two inputs are high so light travels along PO₂, so that O₁ + O₃ is low.

A=1, B=1, C=1, all the inputs are present and the light is routed along the path PO₃, making output O₁ + O₃ high.

So it is found that the output O₁ + O₃ is high only when odd number of inputs are high which is the property of X-OR operation.

Three input majority gate

A majority gate gives output, the majority of the input condition. If majority of the input is 0, the output is zero and if majority of the input are high, i.e.1, the output is high. This is also called majority function or majority vote. The operation can be obtained by combination O₂ + O₃.

In the input conditions (i). A=0, B=0, C=0. (ii). A=0, B=0, C=1, (iii). A=0, B=1, C=0, (iv). A=1, B=0, C=0, the majority are 0 or low inputs. In these conditions no light travels along the path O₂ or O₃, making output O₂ + O₃ low, i.e. majority input.

For others conditions (v) A=0, B=1, C=1, (vi). A=1, B=0, C=1, (vii). A=1, B=1, C=0, (viii). A=1, B=1, C=1, majority of the input is high. For conditions (v) to (vii), the output O₂ is high and for the condition (viii), the output O₃ is high. So for all four conditions (v) to (viii) the combination O₂ + O₃ is high as majority of the inputs are high.

Half Adder

A half adder adds two single bits A and B and generates carry=A AND B and SUM=A X-OR B. As explained in section 4.1 and 4.2 of this communication when input C=0, the outputs O₂ and O₁ produces

CARRY and SUM respectively. Similarly when C=1, the CARRY and SUM are generated from outputs O₃ and O₂ as shown in the block diagram of Figure 6. So in both the conditions of C=0, and C=1 we have half adder operation. So the module can simultaneously gives three input logic gates and half adder. In Figure 6, when C=0, O₁ gives the SUM and O₂ gives the CARRY. But when C=1, O₂ gives the SUM and O₃ gives the CARRY of the half adder. The operation of the half adder can be easily verified from the Table 2.

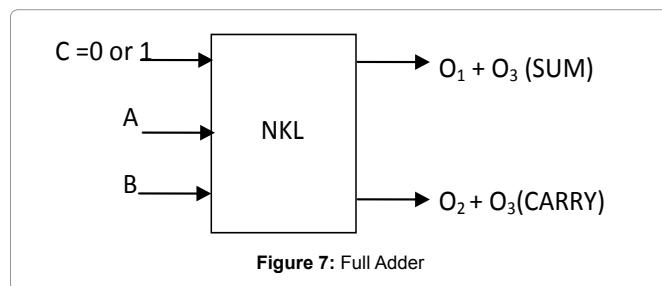
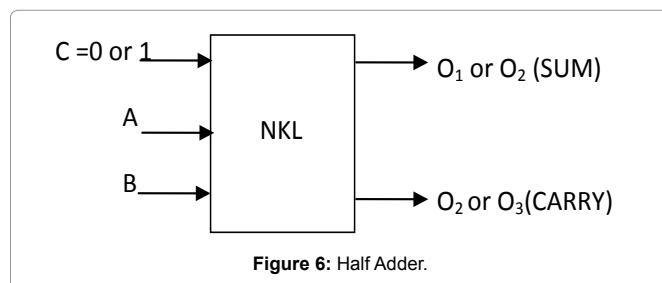
Implementation of the full Adder

The CARRY of a Full Adder is nothing but the majority vote of two input bit A and B and the CARRY of the previous addition which is denoted by C in this case. The sum of a Full Adder is the X-OR operation of the two input bits A and B, and CARRY, C of the previous addition. In logical form

$$\text{SUM} = \text{A X-OR B X-OR C}$$

$$\text{CARRY} = \text{AB} + \text{AC} + \text{BC} \text{ (Majority Function gate).}$$

As explained in section 4.9, the output combination O₁+O₃ gives three input X-OR operation of A, B and C and in section 4.10, it is explained that the three input majority function can be generated from the combination O₂+O₃. Therefore, the full adder block can be drawn as Figure 7. The operation of the full adder is clear from the Table 2.



Conclusions and Discussions

The design and analysis of a nonlinear Kerr lens using Carbon di Sulfide (CS₂) is explained. Nonlinear properties of few other important materials are also included. The variation of nonlinear focal length, change in focal length and angular deviation is plotted against intensity of incident light and better performance in comparison to slab type of nonlinear material in terms of deviation of light is obtained. The deviation produced by the lens is not dependent on the angle of incidence as in nonlinear prism. Further, we can engineer the lens by changing the radii of curvature of the refracting surfaces as well. The most interesting characteristics of the proposed module is that, it can generate all the logic gates, i.e. two input AND, X-OR, NAND, NOR, X-NOR, three input AND, X-OR and majority function and

optical processors half Adder, Full Adder simultaneously. Another interesting fact about the module designed in this communication is that two input logic gates can be implemented in a controlled way, i.e. when C=0, one output gives a two input logic gate and for C=1, the same output gives another logic gate. This confirms reconfigurability of the logic gates also. For example, when C=0, O₁ generates X-OR operation but when C=1, it generates NOR operation as clear from the sections 4.2 and 4.3. This is true for other outputs also. This property of the output O₂ gives very interesting property to the Half Adder. By controlling the input C one can generate SUM and CARRY of the half Adder from a single output O₂. This is possible because O₂ gives X-OR operation (SUM) when C=0 and gives AND operation (CARRY) when C=1 respectively. The device presented in this communication can be used as a binary logic and arithmetic unit that can generate all functionalities simultaneously and can demand novelty in its own characteristics.

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