



## Quantum-Cosmos Nexus Theory

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### Abstract

The Quantum-Cosmos Nexus Theory delves into the intricate web of relationships that tie together fundamental constants, cosmological properties, and the boundaries of our comprehension in the realm of physics. It unveils a profound interconnection between the gravitational constant ( $G$ ), the speed of light ( $c$ ), and the parameters of the observable universe.

It introduces a unification equation that hints at a connection between the fundamental constants. It also introduces a new constant,  $\hbar_{\text{Max}}$ , which is similar to the Planck constant but, on a large scale, signifies the ultimate unit of action or energy on a cosmic scale. With this new constant, new units similar to Planck units have been introduced. They are the equivalence of Planck units in the sense that they represent the limits of our current understanding of physics on the largest scale. The theory also shows that most of the fundamental constants of nature, including the gravitational constant ( $G$ ), the speed of light ( $c$ ), vacuum permittivity ( $\epsilon_0$ ), vacuum permeability ( $\mu_0$ ), the Boltzmann constant ( $k_B$ ), and the fine-structure constant ( $\alpha$ ), can be derived from these new units and Planck units. The first derived equation suggests a potential weakening of the gravitational constant over time, assuming the density remains relatively constant. Although this is a matter of speculation, it has the potential to explain observations related to dark matter. The theory also makes use of the Planck force, defining it as the maximum force on the quantum and cosmic scales. It also emphasizes that the Planck scale is not the ultimate limit and reveals our observational constraints, offering a unique perspective on the universe's fundamental workings. The Quantum-Cosmos Nexus theory reveals how fundamental constants, cosmic dynamics, and the limits of our understanding converge, opening the door to fresh perspectives on the underlying principles of the universe.

**Keywords:** Quantum-Cosmos Nexus; Fundamental constants; Cosmic dynamics; Unification equation

### Introduction

The Quantum-Cosmos Nexus theory presents a compelling exploration of the intricate relationship between the fundamental constants of the universe, encompassing both the quantum and cosmic

scales. This theory delves into the profound interconnections that exist among key constants, such as the gravitational constant, the speed of light, and various Planck and cosmic units, shedding new light on their intrinsic ties.

As we delve into the depths of this theory, it is crucial to first confront the enigma of the gravitational constant, symbolized as  $G$ , which has persisted since Sir Isaac Newton first laid the foundations of gravitational theory in 1665 [1]. Over centuries of scientific progress, our understanding of why  $G$  assumes its specific numerical value remains incomplete. We have gleaned knowledge of  $G$  exclusively through meticulous measurements and experiments, emphasizing the depth of our cosmic ignorance and our enduring quest to decipher the fundamental laws governing our universe.

In the mid-20<sup>th</sup> century, the illustrious physicist Paul Dirac introduced the large number hypothesis, sparking intrigue within the scientific community [2]. This hypothesis hinted at a potential connection between two seemingly unrelated cosmic constants:  $G$  and the age of the universe.

Dirac's insight derived from the observation that certain significant numerical ratios in physics, such as the age of the universe and the strength of gravitational forces, shared a comparable order of magnitude. While the large number hypothesis did not lead to a universally accepted theory, it underscored Dirac's innovative thinking and the ongoing pursuit of uncovering hidden connections within the universe.

Building on this historical perspective, we venture further into the realm of gravitational theory with Gunnar Nordstrom, an early 20<sup>th</sup> century Finnish theoretical physicist. Nordstrom's unconventional proposal suggested that the gravitational constant, a cornerstone of physics determining the strength of gravitational forces, might depend on the distribution of matter throughout the universe [3]. This concept challenged the established principles of gravity, particularly Einstein's theory of general relativity. While it did not supplant Einstein's theory, Nordstrom's work provided valuable insights into alternative approaches to understanding gravity, reflecting the spirit of exploration and innovation that propels scientific progress. In the 1960's, Robert H. Dicke and Carl H. Brans introduced the Brans-Dicke theory of gravitation [4]. Departing from traditional views, this theory introduced a scalar field, 'phi,' capable of varying with time, resulting in fluctuations in gravity's strength. This notion defied the notion of gravity as a fixed and unchanging force, opening the door to the idea that gravity's fundamental nature might evolve over time. While not supplanting general relativity, the Brans-Dicke theory enriched our exploration of gravitational physics, exemplifying scientific inquiry's boldness in questioning established paradigms.

Some theoretical physicists, working within frameworks such as string theory and theories involving extra dimensions, have suggested that fundamental constants, including gravity's strength, might not be as constant as traditionally believed [5]. These speculations challenge our conventional understanding, hinting at a dynamic universe where gravity could vary under different cosmic conditions, reflecting the adventurous spirit of theoretical physics and its ongoing exploration of the universe's fundamental forces.

In the realm of cosmological models, the concept of time-varying gravitational coupling has garnered attention. Various scientists have contributed insights to our evolving understanding of how gravity, a

fundamental cosmic force, may not be immutable but subject to change over time [6,7]. Their collective efforts illuminate the dynamic nature of cosmological research, as scientists continue their quest to unravel the mysteries of our ever-changing cosmos.

The speed of light, denoted as 'c,' stands as a fundamental constant precisely measured in the late 19<sup>th</sup> century [8]. While its value is known, the specific reason for 'c' holding that exact numerical value remains an intriguing enigma. Despite meticulous measurements, the origins of this constant continue to captivate our scientific curiosity.

In summary, the Quantum-Cosmos Nexus theory emerges as a response to a series of fundamental questions. Delving deep into the heart of our universe, this theory sets out to uncover the origins of key constants like the gravitational constant and the speed of light, shedding light on their mysterious values that underpin the very laws of nature. Intriguingly, it asks whether, just as there are limits to our understanding at the subatomic scale, there might exist an upper threshold to our cosmic knowledge. Does the universe conceal its deepest secrets, beyond which our comprehension may never extend? The theory also ventures into the realms of the quantum and cosmic scales, probing the existence of a constant that represents the largest unit of action, akin to the reduced Planck constant's role on the smallest scale proposed by the physicist Max Karl Ernst Ludwig Planck [9]. In doing so, it seeks to establish a profound connection between these two seemingly disparate worlds, unravelling the threads that unite them.

Furthermore, the Quantum-Cosmos Nexus theory endeavours to derive the critical constants of nature, spanning the expanse from cosmic to quantum scales, fostering a comprehensive understanding of how these constants interrelate.

The intriguing question of whether the gravitational constant weakens over time introduces a provocative notion, offering a potential explanation for enigmatic cosmic phenomena like the early universe's structural formations and the elusive nature of dark matter.

Exploring the meaning and purpose of the Planck force, this theory ponders whether it signifies the maximum force achievable on a cosmic scale, unravelling its significance in the grand tapestry of universal laws. In the pursuit of knowledge, it questions whether the Planck length is truly the ultimate limit in our quest to fathom the fabric of space and time.

Lastly, it seeks to unravel the ultimate structure of the Planck and cosmic scales, providing an illuminating insight into their foundational nature. The Quantum-Cosmos Nexus theory stands as a beacon of inquiry, beckoning us to explore the boundaries of our cosmic understanding, and its quest to uncover answers to these profound questions holds the promise of a new era of enlightenment and discovery in the realms of physics and cosmology.

## Materials and Methods

We will start with Newton's gravitational constant (G), which has the unit

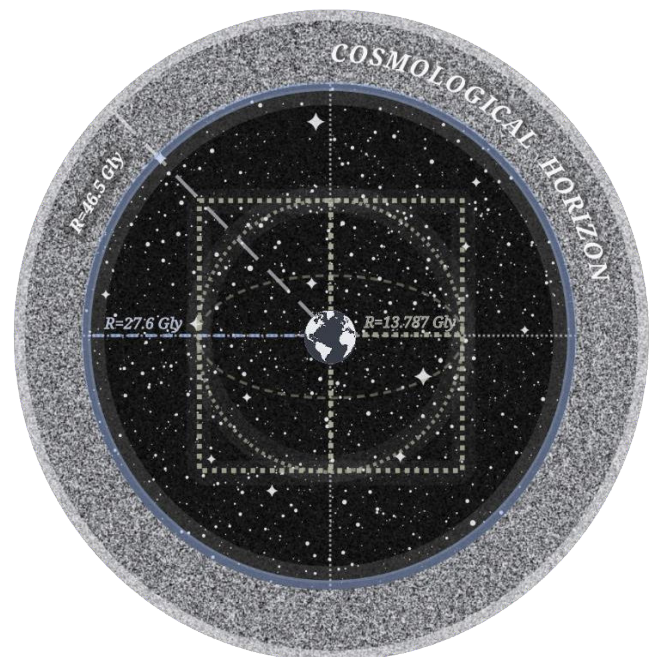
$$\frac{Nm^2}{kg^2} = \frac{m^3}{kg \cdot s^2}$$

by deriving an equation from these units.  $m^3$  is the unit of volume V, kg is unit of mass M and s is the unit of time t. We get the gravitational clock equation:

$$G = \frac{V}{M \cdot t^2} = \frac{R^3}{M \cdot t^2} \quad (1)$$

Upon substituting the established value of the age of the universe [10] and  $G \approx 6.6743 \cdot 10^{-11} m^3 \cdot kg^{-1} \cdot s^{-2}$ , resolving for both mass and volume, and then striving to achieve equilibrium within the equation, our objective is to attain the precise value of the gravitational constant [11]. We find that the radius is equal to the Hubble radius (all the upcoming units and parameters have been named in honor of the esteemed astronomer Edwin Hubble) (Figure 1):

$$R_H = 1.30435091 \cdot 10^{26} \text{ meters} \\ = 13.787 \text{ billion light years}$$



**Figure 1:** illustrates the difference in size between the Hubble cube and the cosmological horizon (light from the CMB), which has a radius of approximately 46.508 billion light years

With a cubic volume equal to the Hubble radius cubed:

$$V_H = R_H^3 = 2.21913302 \cdot 10^{78} m^3$$

The mass of the Hubble cube is:

$$M_H = 1.75642709 \cdot 10^{53} kg$$

The age of the universe (Hubble time): 1 year  $\approx$  31557600 seconds s [11]

$$\text{Age (in seconds)} \quad t_H = 13.787 \text{ billion years} \cdot \frac{1,000,000,000 \text{ years}}{\text{billion years}} \cdot 31557600 \frac{\text{seconds}}{\text{years}} \\ t_H \approx 4.35084631 \cdot 10^{17} \text{ seconds}$$

$$G = \frac{V_H}{M_H \cdot t_H^2}$$

$$= \frac{2.21913302 \cdot 10^{78}}{1.75642709 \cdot 10^{53} \cdot (4.35084631 \cdot 10^{17})^2}$$

$$= 6.6743 \cdot 10^{-11} m^3 \cdot kg^{-1} \cdot s^{-2}$$

### Density of the Hubble Cube $\rho_H$

$$\rho_H = \frac{M_H}{V_H} = \frac{\text{Mass of the Hubble sphere}}{\text{Volume of the Hubble sphere}}$$

$$= \frac{1.75642709 \cdot 10^{53}}{2.21913302 \cdot 10^{78}} = 7.91492477 \cdot 10^{-26} \frac{kg}{m^3}$$

$$\rho_H^{-1} = \frac{V_H}{M_H} = 1.26343589 \cdot 10^{25} \frac{m^3}{kg}$$

$$G = \frac{1}{\rho_H \cdot t_H^2} \quad (2)$$

After solving the gravitational clock equation for  $t_H$ , substituting  $t_H$  for  $a/v$ , and then solve for  $v$ , the speed of light is calculated ( $v=c$ ), ( $d=R_H$ ).

$$t_H^2 = \frac{1}{\rho_H \cdot G} \rightarrow \frac{R_H^2}{c^2} = \frac{1}{\rho_H \cdot G}$$

$$c = \pm \sqrt{\rho_H \cdot G \cdot R_H^2} \quad (2)$$

$$c = \pm 299792458.1 \frac{m}{s}$$

By applying the speed of light equation, which relates speed of light  $c$ , vacuum permittivity  $\epsilon_0$ , and vacuum permeability  $\mu_0$  [12]. We get unification between the fundamental constants.

$$c = \frac{1}{\sqrt{\mu_0 \cdot \epsilon_0}}$$

$$\frac{1}{\sqrt{\mu_0 \cdot \epsilon_0}} = \sqrt{\rho_H \cdot G \cdot R_H^2} \quad (3)$$

### 'Unification Equation'

$$1 = G \cdot \rho_H \cdot R_H^2 \cdot \mu_0 \cdot \epsilon_0 \quad (4)$$

Applying the speed of light equation

$$\frac{1}{c^2} = \mu_0 \cdot \epsilon_0 \text{ and the gravitational clock equation } \Delta G = \frac{1}{\rho_H \cdot \Delta t_H^2} \text{ to the unification}$$

equation reveals the relationship between the speed of light, the Hubble radius, and the age of the universe.

$$1 = \frac{1}{\rho_H \cdot \Delta t_H^2} \cdot \rho_H \cdot R_H^2 \cdot \frac{1}{c^2}$$

$$\Delta c^2 = \frac{\Delta R_H^2}{\Delta t_H^2}$$

$$c = H_0 \cdot R_H = \frac{R_H}{t_H} = \frac{1.30435091 \cdot 10^{26} m}{4.35084631 \cdot 10^{17} s} \quad (5)$$

$$c = 299792458.1 m \cdot s^{-1}$$

According to the formula, the length of the Hubble radius is always the same as the radius of the universe's 4-sphere and both are rising at the speed of light; thus, both are increasing in length by one light-year every year. However, the two are not equivalent. (The radius of the 4-sphere is in 4D space, whereas the Hubble radius is in 3D space.)

### Planck units' relationship with the Hubble parameters

By integrating the gravitational clock equation (1) and equation (6) with Planck units [13], we attain the connection between Planck units and the Hubble parameters.

$$l_{Planck} = \sqrt{\frac{\hbar \cdot G}{c^3}} = \sqrt{\frac{\hbar}{c^3 \cdot \rho_H \cdot t_H^2}} = \sqrt{\frac{\hbar \cdot t_H}{R_H^3 \cdot \rho_H}} \quad (6)$$

$$\Delta l_{Planck} = 1.61625502 \cdot 10^{-35} \text{ m}$$

$$t_{Planck} = \sqrt{\frac{\hbar \cdot G}{c^5}} = \sqrt{\frac{\hbar}{c^5 \cdot \rho_H \cdot t_H^2}} = \sqrt{\frac{\hbar \cdot t_H^3}{R_H^5 \cdot \rho_H}} \quad (7)$$

$$= 5.39124644 \cdot 10^{-44} \text{ s}$$

$$T_{Planck} = \sqrt{\frac{\hbar \cdot c^5}{G \cdot K_B^2}} = \sqrt{\frac{\hbar \cdot c^5 \cdot \rho_H \cdot t_H^2}{K_B^2}} = \sqrt{\frac{\hbar \cdot R_H^5 \cdot \rho_H}{t_H^3 \cdot K_B^2}} \quad (9)$$

$$= 1.41678416 \cdot 10^{32} \text{ K}$$

$$m_{Planck} = \sqrt{\frac{\hbar \cdot c}{G}} = \sqrt{\hbar \cdot c \cdot \rho_H \cdot t_H^2} = \sqrt{\hbar \cdot R_H \cdot \rho_H \cdot \Delta t_H} \quad (8)$$

$$= 2.17643434 \cdot 10^{-8} \text{ kg}$$

## Reduced Planck constant integration

$$\hbar = \frac{m_p \cdot l_p^2}{t_p} \text{ kg} \cdot \text{m}^2 \cdot \text{s}^{-1} \quad (9)$$

$$l_p = \sqrt{\frac{\hbar \cdot \Delta t_H}{R_H^3 \cdot \rho_H}} = \sqrt{\frac{m_p \cdot l_p^2 \cdot t_H}{t_p \cdot R_H^3 \cdot \rho_H}}$$

$$1. \quad t_p \cdot R_H^3 \cdot \rho_H = m_p \cdot t_H \quad (10)$$

$$t_p = \frac{m_p \cdot t_H}{R_H^3 \cdot \rho_H} = \sqrt{\frac{\hbar \cdot \Delta t_H^3}{R_H^5 \cdot \rho_H}} = \sqrt{\frac{m_p \cdot l_p^2 \cdot t_H^3}{t_p \cdot R_H^5 \cdot \rho_H}}$$

$$\frac{m_p^2 \cdot t_H^2}{R_H^6 \cdot \rho_H^2} = \frac{m_p \cdot l_p^2 \cdot t_H^3}{t_p \cdot R_H^5 \cdot \rho_H}$$

$$2. \quad m_p \cdot t_p = l_p^2 \cdot R_H \cdot \rho_H \cdot t_H \quad (11)$$

By solving equation one and two for  $m_p$ :

$$m_p = \frac{l_p^2 \cdot R_H \cdot \rho_H \cdot t_H}{t_p} = \frac{t_p \cdot R_H^3 \cdot \rho_H}{t_H}$$

$$l_p^2 \cdot t_H^2 = t_p^2 \cdot R_H^2$$

$$\frac{l_p}{t_p} = \frac{R_H}{t_H} \quad (12)$$

$$R_H = \frac{t_H \cdot l_p}{t_p} = 1.30435091 \cdot 10^{26} \text{ m}$$

## Largest Quanta $\hbar_{Max}$

The Planck constant [9] (denoted as " $\hbar$ ") is often regarded as the fundamental constant that sets the scale for the smallest possible quanta in quantum mechanics. It plays a crucial role in quantum physics and defines the smallest unit of action in the universe. The Planck constant, along with other fundamental constants like the speed of light ( $c$ ) and the Gravitational constant ( $G$ ), defines the Planck units, which are natural units for various physical quantities.

We can derive the largest quanta possible by simply looking at the units of the reduced Planck constant that have been proposed by Max Karl Ernst Ludwig Planck and replacing the units with the calculated Hubble parameters  $M_H$ ,  $R_H$ ,  $t_H$ .

$\hbar$  has the units  $kg \cdot m^2 \cdot s^{-1}$

$$\hbar_{Max} = \frac{M_H \cdot R_H^2}{t_H} = 6.86823704 \cdot 10^{87} kg \cdot m^2/s \quad (15)$$

### Hubble Units

Hubble Length:

$$R_H = \sqrt{\frac{\hbar_{Max} \cdot G}{c^3}} = 1.30435091 \cdot 10^{26} m \quad (16)$$

Hubble Time:

$$t_H = \sqrt{\frac{\hbar_{Max} \cdot G}{c^5}} = 4.35084631 \cdot 10^{17} s \quad (17)$$

Hubble Temperature:

$$T_H = \sqrt{\frac{\hbar_{Max} \cdot c^5}{G \cdot K_B^2}} = 1.14337384 \cdot 10^{93} K \quad (18)$$

Hubble Mass:

$$M_H = \sqrt{\frac{\hbar_{Max} \cdot c}{G}} = 1.75642709 \cdot 10^{53} kg \quad (19)$$

Hubble Charge:

$$q_H = \sqrt{\epsilon_0 \cdot \hbar_{Max} \cdot c} = 4.26979824 \cdot 10^{42} C \quad (20)$$

Hubble Area:

$$A_H = R_H^2 = \frac{\hbar_{Max} \cdot G}{c^3} = 1.70133129 \cdot 10^{52} m^2 \quad (21)$$

Hubble Volume:

$$V_H = \sqrt{\frac{(\hbar_{Max} \cdot G)^3}{c^9}} = 2.21913302 \cdot 10^{78} m^3 \quad (22)$$

Hubble Momentum:

$$\vartheta_H = \sqrt{\frac{\hbar_{Max} \cdot c^3}{G}} = 5.26563595 \cdot 10^{61} kg \cdot m \cdot s^{-1} \quad (23)$$

Hubble Energy:

$$E_H = \frac{\hbar_{Max}}{t_H} = \sqrt{\frac{\hbar_{Max} \cdot c^5}{G}} = 1.57859795 \cdot 10^{70} J \quad (24)$$

Hubble Force

$$F_H = \frac{E_H}{R_H} = \frac{\hbar_{Max}}{R_H \cdot t_H} = 1.21025556 \cdot 10^{44} N \quad (25)$$

Hubble Density:

$$\rho_H = \frac{c^5}{\hbar_{Max} \cdot G^2} = 7.91492478 \cdot 10^{-26} kg \cdot m^{-3} \quad (26)$$

Hubble Acceleration

$$a_H = \frac{c}{t_H} = \sqrt{\frac{c^7}{\hbar_{Max} \cdot G}} = 6.89044008 \cdot 10^{-10} m/s^2 \quad (27)$$

## Gravitational constant derivation from Planck's units and Hubble units

$$G = \frac{R_H^3}{M_H \cdot t_H^2} = \frac{l_P^3}{m_P \cdot t_P^2} \quad (28)$$

$$G = 6.6743 \cdot 10^{-11} \text{ m}^3 \cdot \text{kg}^{-1} \cdot \text{s}^{-2}$$

Derivation of vacuum permittivity  $\epsilon_0$ , vacuum permeability  $\mu_0$ , and speed of light from Planck units and Hubble Units [13-15]

$$q_P = \sqrt{\epsilon_0 \cdot \hbar \cdot c} = 5.29081769 \cdot 10^{-19} \text{ C}$$

$$q_H = \sqrt{\epsilon_0 \cdot \hbar_{Max} \cdot c} = 4.26979824 \cdot 10^{42} \text{ C}$$

$$\begin{aligned} \epsilon_0 &= \frac{F}{m} = \frac{s^4 \cdot A^2}{\text{kg} \cdot \text{m}^2} = \frac{s^2 \cdot C^2}{\text{kg} \cdot \text{m}^3} \\ \epsilon_0 &= \frac{q_P^2 \cdot t_P^2}{m_P \cdot l_P^3} = \frac{q_H^2 \cdot t_H^2}{M_H \cdot R_H^3} \\ &= 8.85418891 \cdot 10^{-12} \text{ F} \cdot \text{m}^{-1} \end{aligned} \quad (29)$$

$$\begin{aligned} \mu_0 &= \frac{N}{A^2} = \frac{\text{kg} \cdot \text{m}}{s^2 \cdot A^2} = \frac{\text{kg} \cdot \text{m}}{C^2} \\ \mu_0 &= \frac{m_P \cdot l_P}{q_P^2} = \frac{M_H \cdot R_H}{q_H^2} \\ &= 1.25663691 \cdot 10^{-6} \text{ N} \cdot \text{A}^{-2} \end{aligned} \quad (30)$$

$$c^2 = \frac{1}{\mu_0 \cdot \epsilon_0}$$

$$c^2 = \frac{q_P^2}{m_P \cdot l_P} \cdot \frac{m_P \cdot l_P^3}{q_P^2 \cdot t_P^2}$$

$$c = \frac{l_P}{t_P} = \frac{1.61625502 \cdot 10^{-35}}{5.39124644 \cdot 10^{-44}}$$

$$= 299792457.6 \frac{\text{m}}{\text{s}}$$

$$c = \frac{l_{Planck}}{t_{Planck}} = \frac{R_{Hubble}}{t_{Hubble}} \quad (31)$$

## Boltzmann constant derivation from Planck units and Hubble units

$$K_B = \frac{J}{K} = \frac{\text{kg} \cdot \text{m}^2}{\text{K} \cdot \text{s}^2}$$

$$K_B = \frac{m_P \cdot l_P^2}{T_P \cdot t_P^2} = \frac{M_H \cdot R_H^2}{T_H \cdot t_H^2} = \frac{m_P \cdot c^2}{T_P} = \frac{M_H \cdot c^2}{T_H} \quad (32)$$

$$K_B = 1.380649 \cdot 10^{-23} \text{ J} \cdot \text{K}^{-1}$$

## Unification equation application

By applying the unification equation to solve for 'G,' followed by a similar approach with Newton's law of universal gravitation [1]. Subsequently, we merge these two equations to provide a fresh perspective on the law of universal gravitation.

$$G = \frac{F_g \cdot d^2}{M_1 \cdot m_2} = \frac{1}{\rho_H \cdot R_H^2 \cdot \mu_0 \cdot \epsilon_0}$$

$$F_g = \frac{M_1 \cdot m_2}{d^2 \cdot \rho_H \cdot R_H^2 \cdot \mu_0 \cdot \epsilon_0} = \frac{M_1 \cdot m_2}{d^2 \cdot \rho_H \cdot t_H^2} \quad (33)$$

We do the same thing again for Coulomb's law for electrostatic force [16] by solving for  $\epsilon_0$ .

$$\epsilon_0 = \frac{q_1 \cdot q_2}{4 \cdot \pi \cdot d^2 \cdot F_c} = \frac{1}{G \cdot \rho_H \cdot R_H^2 \cdot \mu_0}$$

$$\begin{aligned} F_c &= \frac{q_1 \cdot q_2 \cdot G \cdot \rho_H \cdot R_H^2 \cdot \mu_0}{4 \cdot \pi \cdot d^2} = \frac{q_1 \cdot q_2 \cdot R_H^2 \cdot \mu_0}{4 \cdot \pi \cdot d^2 \cdot t_H^2} \\ &= \frac{q_1 \cdot q_2 \cdot c^2 \cdot \mu_0}{4 \cdot \pi \cdot d^2} \end{aligned} \quad (34)$$

Now for Coulomb's laws of magnetic force [17] by solving for  $\mu_0$ .

$$\mu_0 = \frac{4 \cdot \pi \cdot d^2 \cdot F_{ma}}{m_{a1} \cdot m_{a2}} = \frac{1}{G \cdot \rho_H \cdot R_H^2 \cdot \epsilon_0}$$

$$F_{ma} = \frac{m_{a1} \cdot m_{a2}}{4 \cdot \pi \cdot d^2 \cdot G \cdot \rho_H \cdot R_H^2 \cdot \epsilon_0} = \frac{m_{a1} \cdot m_{a2}}{4 \cdot \pi \cdot d^2 \cdot c^2 \cdot \epsilon_0} \quad (35)$$

We can merge the three equations into the unification equation.

$$1 = \frac{F_g \cdot d^2}{M_1 \cdot m_2} \cdot \frac{q_1 \cdot q_2}{4 \cdot \pi \cdot d^2 \cdot F_c} \cdot \frac{4 \cdot \pi \cdot d^2 \cdot F_{ma}}{m_{a1} \cdot m_{a2}} \cdot \rho_H \cdot R_H^2$$

$$\frac{F_c}{F_g \cdot F_{ma}} = d^2 \cdot \frac{q_1 \cdot q_2}{(M_1 \cdot m_2) \cdot (m_{a1} \cdot m_{a2})} \cdot \rho_H \cdot R_H^2$$
(36)

The integration of Newton's law of universal gravitation and Coulomb's law into the unification equation provides the strength ratio between the gravitational force and the Coulomb's force.

$$1 = G \cdot \rho_H \cdot R_H^2 \cdot \mu_0 \cdot \varepsilon_0$$
(37)

$$1 = \frac{F_g \cdot d^2}{M_1 \cdot m_2} \cdot \frac{q_1 \cdot q_2}{4 \cdot \pi \cdot d^2 \cdot F_c} \cdot \rho_H \cdot R_H^2 \cdot \mu_0$$

$$\frac{F_c}{F_g} = \frac{q_1 \cdot q_2}{4 \pi \cdot M_1 \cdot m_2} \cdot \rho_H \cdot R_H^2 \cdot \mu_0$$
(38)

We can calculate the strength ratio by plugging in the charge and mass of the electron and proton.

Mass of the electron is  $m_e = 9.1093837 \cdot 10^{-31} \text{ kg}$

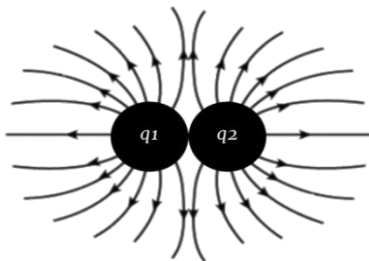
Mass of the proton is  $m_{pro.} = 1.67262192 \cdot 10^{-27} \text{ kg}$

Proton/Electron charge  $q = \pm 1.60217663 \cdot 10^{-19} \text{ C}$

$$\frac{F_c}{F_g} = 2.26866143 \cdot 10^{39}$$

### Fine-structure constant

We will start by calculating the classical radius of the electron and proton (Figure 2).



**Figure 2:** Illustrates two electrons with their repulsive field lines separated by a distance equal to one electron's diameter

Let's picture two electrons touch each other, meaning they are separated by one electron diameter as shown in Figure 2. If we

assume, for simplicity, that the electron  $q_1$  is stationary, the force felt by the second electron

$$q_2 \text{ is } F = \frac{m \cdot c^2}{r}$$
(39)

and the force is also equal to the Coulomb force

$$F_c = \frac{q^2}{4 \cdot \pi \cdot \varepsilon_0 \cdot r^2}$$
(40)

Now we do the same for the proton radius  $r_{pro.}$  ( $m_{pro.}$  Not be confused with Planck mass  $m_p$ )

$$r_{pro.} = \frac{q_{1,2}^2}{4 \pi \cdot \varepsilon_0 \cdot m_{pro.} \cdot c^2}$$

$$r_{pro.} = 1.53469826 \cdot 10^{-18} \text{ m}$$

Now

$$r_e \cdot m_e = 2.56696996 \cdot 10^{-45} \text{ kg} \cdot \text{m}$$

and

$$r_{pro.} \cdot m_{pro.} = 2.56696996 \cdot 10^{-45} \text{ kg} \cdot \text{m}$$

Therefore

$$r_e \cdot m_e = r_{pro} \cdot m_{pro} \quad (42)$$

Relation with Planck units

$$m_p \cdot l_p = 3.51767293 \cdot 10^{-43} \text{ kg} \cdot \text{m}$$

$$\alpha = \frac{r_e \cdot m_e}{m_p \cdot l_p} = \frac{r_{pro} \cdot m_{pro}}{m_p \cdot l_p} = \frac{1}{137} \quad (43)$$

$$\frac{r_e \cdot m_e}{m_p \cdot l_p} = \frac{r_{pro} \cdot m_{pro}}{m_p \cdot l_p} = \frac{e^2}{4\pi \cdot \epsilon_0 \cdot \hbar \cdot c} \quad (44)$$

after substituting equations (11) and (29)

$$\begin{aligned} \alpha &= \frac{e^2 \cdot l_p^2}{4\pi \cdot q_p^2 \cdot t_p^2 \cdot c^2} \\ \frac{l_p^2}{t_p^2} &= c^2 \\ \alpha &= \frac{e^2}{4\pi \cdot q_p^2} \end{aligned} \quad (45)$$

Relation with Hubble units

$$e_H = q_H \cdot \sqrt{4\pi \cdot \alpha} \quad (46)$$

$$\alpha = \frac{e_H^2}{4\pi \cdot \epsilon_0 \cdot \hbar_{Max} \cdot c}$$

after substituting equations (15) and (29)

$$\alpha = \frac{e_H^2}{4\pi \cdot q_H^2} \quad (47)$$

$$\frac{e^2}{q_p^2} = \frac{e_H^2}{q_H^2} \quad (48)$$

$$\frac{r_e \cdot m_e}{m_p \cdot l_p} = \frac{r_{pro} \cdot m_{pro}}{m_p \cdot l_p} = \frac{e_H^2}{4\pi \cdot \epsilon_0 \cdot \hbar_{Max} \cdot c} \quad (49)$$

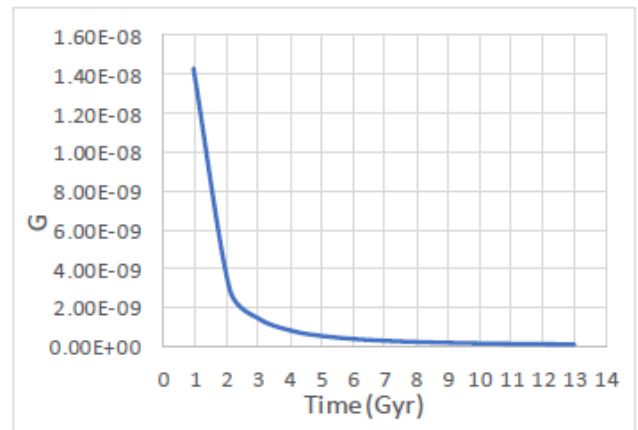
### Potential change in the gravitational constant

The gravitational clock equation suggests a potential variation in the gravitational constant over time. Assuming the density of the

Hubble cube remains relatively constant; we can calculate this change in the gravitational constant.

A change in the gravitational constant, G, has the potential to offer an alternative explanation for dark matter by reevaluating our understanding of this fundamental constant. Although this remains a matter of speculation. It is worth investigating further. Unfortunately, I have been unable to locate the necessary data to support this hypothesis through calculations. I hope that experts will test this equation by incorporating a calculated value for G at each specific time when conducting calculations for galaxy rotation curves (Figure 3).

$$\Delta G = \frac{1}{\rho_H \cdot \Delta t_H^2} \quad (2)$$



**Figure 3:** Shows the decrease of the gravitational constant G from 1 to 13 billion years after the Big Bang (Most of the galaxies in the universe, as we know them today, began to take shape approximately 1 to 2 billion years after the Big Bang).

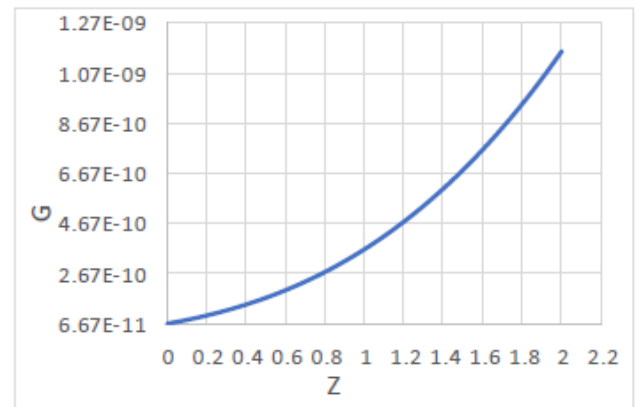
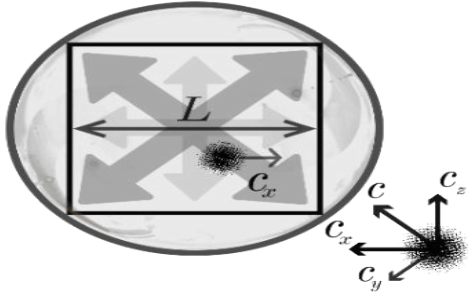


Figure 4: illustrates the increase in the gravitational constant (G) as Redshift z increases. (Calculated with  $\Omega_M=0.286$ ,  $\Omega_{Vac}=0.714$  and  $H_0=69.6$ )

### Calculation of the Hubble cube pressure (Energy Density)

As photons lack both mass and volume, yet carry momentum and can't directly interact with each other, we can think of them as representations of pure kinetic energy. With this idea, picture a single

photon held within the Hubble cube. It has an x-direction in its velocity. (We can refer to it as the velocity of light, considering that we are discussing the phase velocity with which wave fronts propagate (Figure 5).



**Figure 5:** shows the X, Y, and Z velocity components of a photon inside the Hubble cube

This interpretation is essential to account for the  $\pm$  sign that arises from the calculations of the speed of light. However, it's important to note that when we shift our focus to the group velocity, we are essentially determining the speed at which intensity propagates.). Keeping in mind that a photon can have a velocity in any direction, that velocity will have X, Y, and Z components. Since they don't interact, all of them have X, Y, and Z components (Figure 5) in their velocity:

$$c_x^2 = c_y^2 = c_z^2$$

$$\text{Momentum: } \theta = m \cdot c_x,$$

$$\text{change in Momentum: } \Delta\theta = 2 \cdot m \cdot c_x$$

$$\text{Impulse: } I = \Delta\theta = F \cdot \Delta t$$

Since the photon is traveling from one end of the interior surface of the Hubble cube (Figure 5) to the other end and back, we know that it only happens once every time it travels twice across the length of the cube interior.

$$F = \frac{\Delta\theta}{\Delta t} = \frac{2 \cdot m \cdot c_x}{\Delta t} \rightarrow t = \frac{d}{c_x} = \frac{2L}{c_x} \rightarrow F = \frac{m \cdot c_x^2}{L}$$

This is for only one photon in the x direction, but if we take all the photons into account and they all go in different directions, we can say:

Now we replace  $c_x^2$  by  $c_{total}^2 \rightarrow F = \frac{m \cdot c_{total}^2}{L}$   
now the pressure (energy density):

$$P_H = \frac{F}{A} = \frac{m \cdot c^2}{L \cdot L^2} = \frac{M_H \cdot c_{total}^2}{V_H} \quad (21)$$

we plug in the mass  $M_H$  and the volume  $V_H$  of the Hubble cube:

$$P_H = \frac{1.75642709 \cdot 10^{53}}{2.21913302 \cdot 10^{78}} \cdot (299792458)^2$$

$$= 7.11357963 \cdot 10^{-9} \text{ Pa}$$

$$E_H = P_H \cdot V_H = M_H \cdot c^2$$

#### United force $F_{Max}$

If skepticism arises regarding the accuracy of this pressure value, let me introduce a new method for discerning the accuracy and authenticity of most cosmological parameters inside the Hubble cube. Using Planck units and the known parameters of the Hubble cube.

$$F_{Max} = F_H = \frac{M_H \cdot R_H}{t_H^2} = \frac{m_p \cdot l_p}{t_p^2} = \frac{E_p}{l_p} = \frac{E_H}{R_H} \quad (51)$$

$$F_{Max} = 1.21025556 \cdot 10^{44} \text{ N}$$

Now, by simply analyzing the pressure unit (energy density), we can derive an equation to apply the maximum force.

$$1Pa = \frac{N}{m^2} = \frac{F_{Max}}{R_H^2}$$

$$\frac{F_{Max}}{R_H^2} = \frac{1.21025556 \cdot 10^{44}}{(1.30435091 \cdot 10^{26})^2}$$

$$P_H = 7.11357963 \cdot 10^{-9} Pa$$

#### Waves equation

The Newton-Laplace equation is a fundamental concept in physics that originally emerged in the context of acoustics, describing how waves propagate through a medium such as air or water. However, its applicability is not limited to sound; it can also be extended to describe the behavior of light. Given that we have calculated the density and pressure of the Hubble cube, we can apply the wave equation to calculate the speed of light [18].

$$c = \sqrt{\frac{P_H}{\rho_H}} = \frac{7.11357963 \cdot 10^{-9}}{7.91492477 \cdot 10^{-26}} \quad (52)$$

$$= 299792458.1 \text{ m} \cdot \text{s}^{-1}$$

$$c^2 = \frac{1}{\mu_0 \cdot \varepsilon_0} = \frac{P_H}{\rho_H} \quad (53)$$

$$P_H = G \cdot \rho_H^2 \cdot R_H^2 \quad (54)$$

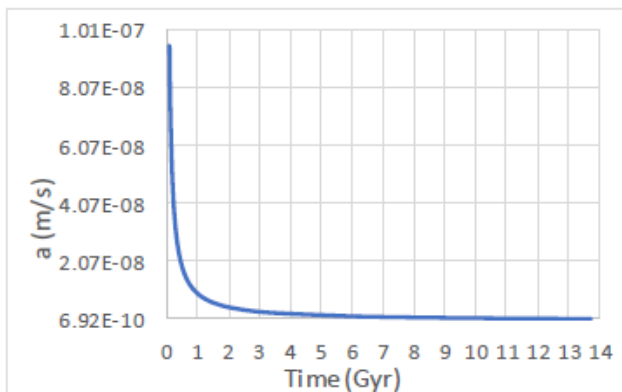
Hubble acceleration  $a_H$

$$a_H = \frac{R_H}{t_H^2} = \frac{c}{t_H} = \frac{299792458}{4.35084631 \cdot 10^{17}} \quad (27)$$

$$= 6.89044008 \cdot 10^{-10} \text{ m} \cdot \text{s}^{-2}$$

Since Planck acceleration is defined as the acceleration from absolute rest to the speed of light in one Planck time, Hubble acceleration can be defined as the acceleration from absolute rest to the speed of light in Hubble time. This does not imply that the speed of light is changing, but rather that the direction of the velocity vector changes over time.

And since the Hubble acceleration is decelerating as the universe ages, this might indicate that space was once curved in the early universe, and it's becoming flatter as the universe ages and expands. As a result, light from very distant galaxies might not travel in a perfectly straight line (Figure 6).



**Figure 6:** illustrates the decrease (deacceleration) of the Hubble acceleration between 0.1 and 13.7 billion years.

Since the Hubble acceleration is calculated, a new formula can be introduced.

$$P_H = \rho_H \cdot R_H \cdot a_H = \rho_H \cdot c^2 \quad (26)$$

$$= 7.11357963 \cdot 10^{-9} \text{ Pa}$$

### Maximum force, energy, and power

**Maximum force:** (For both Hubble and Planck scale)

$$F_{Max} = m_p \cdot a_p = M_H \cdot a_H$$

$$F_{Max} = \frac{h}{l_p \cdot t_p} = \frac{h_{Max}}{R_H \cdot t_H}$$

$$F_{Max} = \frac{E_p}{l_p} = \frac{E_H}{R_H}$$

$$F_{Max} = m_p \cdot \frac{l_p}{t_p^2} = M_H \cdot \frac{R_H}{t_H^2} \quad (55)$$

$$= 1.21025556 \cdot 10^{44} \text{ N}$$

### Maximum Energy

(For the Hubble scale)

$$E_{Max} = P_H \cdot V_H = M_H \cdot c^2$$

$$E_{Max} = M_H \cdot a_H \cdot R_H$$

$$E_{Max} = h_{Max} \cdot f = h_{Max} \cdot \frac{1}{t_H} \quad (56)$$

$$= 1.57859794 \cdot 10^{70} \text{ J}$$

### Maximum Power

(For both Hubble and Planck scale)

$$P = F_{Max} \cdot c = \frac{E_{Max}}{t_H}$$

$$P = \frac{F_{Max} \cdot R_H}{t_H} = \frac{F_{Max} \cdot l_p}{t_p} = \frac{E_p}{t_p} \quad (57)$$

$$= 3.62830244 \cdot 10^{53} \text{ Watt}$$

### Hubble and Planck cubes properties and similarities

Both the Hubble and Planck cubes are hypothetical concepts. The Planck cube is based on the Planck length  $l_p$  and has a volume of

$$V_P = l_P^3 = 4.2217 \cdot 10^{-105} \text{ m}^3$$

The Planck length is not the smallest length possible, and there is no reason or evidence to suggest such a claim, just like the Hubble length (radius) is not the longest possible. In 1973, Jacob Bekenstein published a paper in which he showed that the surface area of a black hole increases by  $1A_P$  for every bit of information which crosses the event horizon.

$$(1A_P = l_P^2)$$

The surface area of a sphere is given by  $4\pi R^2$ . Therefore, the new surface area is given by  $4\pi R_{new}^2 = 4\pi R_{old}^2 + l_P^2$  Then:

$$R_{new} = \sqrt{R_{old}^2 + \frac{l_P^2}{4\pi}}$$

Therefore, the change in radius is given by:

$$\delta R = R_{new} - R_{old}$$

$$\delta R = R_{old} \cdot \sqrt{1 + \frac{l_P^2}{4\pi \cdot R_{old}^2}} - R_{old}$$

We then expand the brackets (since  $R_{old} \gg l_P$  for any Black hole), such that:

$$\delta R \approx R_{old} \left( 1 + \frac{l_P^2}{8\pi \cdot R_{old}^2} \right) - R_{old}$$

Therefore:

$$\delta R \approx \frac{l_P^2}{8\pi \cdot R_{old}} \ll l_P$$

Therefore, via Bekenstein's result, the change in radius of a black hole when 1 bit of information is added is much smaller than 1 Planck length.

The Hubble cube is based on the Hubble length ( $R_H$ ) has a volume of  $V_H = 2.21913302 \cdot 10^{78} \text{ m}^3$ . When we look up at the sky, we see light that's, at most, 13.787 billion years old (As shown in Figure 1), originating from stars and galaxies now positioned around 46.5 billion light years away. Anything beyond this point is beyond our observational horizon. However, each passing second brings us new, even older light from slightly more distant sources. Consequently, our perspective on the cosmos is continually expanding. All we need to do is be patient and observe as the universe ages, allowing light from more distant places the time it needs to reach us. The Hubble distance sets our observational boundary, and this limit is consistent for all observers, regardless of their location within the universe. From each

observer's viewpoint, the observable universe extends to a radius of roughly 13.787 billion light-years.

The Planck length and the Hubble length are both critical in defining observation limits. While the Hubble length sets an upper boundary for what we can observe in the vastness of the cosmos, the Planck length does the same for the subatomic world. Importantly, these limits are consistent for all observers throughout the universe, regardless of their location. And just as the Hubble length doesn't represent the maximum possible distance, the Planck length doesn't signify the smallest conceivable scale. Both of these lengths establish the boundaries of our observations, from the largest cosmic structures to the tiniest quantum realms. First, let's calculate the distance between B and G for the Hubble cube (d) as shown in Figure 7.

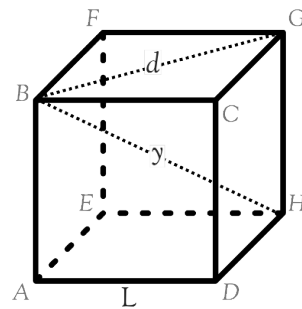


Figure 7: illustrates the longest diagonal (d) for square BCGF and the longest diagonal (y) within the Hubble and Planck cubes

$$L = L_H = R_H$$

$$d_H^2 = L_H^2 + L_H^2 = 2 \cdot L_H^2$$

$$d_H = \sqrt{2 \cdot L_H^2} = 1.84463075 \cdot 10^{26} \text{ m}$$

Now the diagonal between H and B (y) shown in Figure 7

$$y_H^2 = L_H^2 + d_H^2 = L_H^2 + 2 \cdot L_H^2 = 3L_H^2$$

$$y_H = \sqrt{3 \cdot L_H^2} = 2.25920205 \cdot 10^{26} \text{ m}$$

Planck Cube

$$L = l_P$$

$$d_P = \sqrt{2 \cdot l_P^2} = 2.28572977 \cdot 10^{-35} \text{ m}$$

$$y_P = \sqrt{3 \cdot l_P^2} = 2.79943581 \cdot 10^{-35} \text{ m}$$

Both the Hubble and Planck Schwarzschild radii ( $r_{s_H}$ ,  $r_{s_P}$ ), are two times bigger than the Hubble and Planck lengths. (This is just to show similarities and does not necessarily mean anything.)

$$r_{s_H} = \frac{2 \cdot G \cdot M_H}{c^2} = 2 \cdot R_H = \frac{d_H^2}{R_H}$$

$$r_{s_P} = \frac{2 \cdot G \cdot m_P}{c^2} = 2 \cdot l_P = \frac{d_P^2}{l_P}$$

$$\frac{r_{s_P}}{l_P} = \frac{r_{s_H}}{R_H}$$

### Why the ultimate structure of Planck and Hubble scales resembles a cube

**The perpetual reducibility dilemma:** The universe's capacity for perpetual reducibility presents a fundamental challenge. If the universe were perpetually reducible, every event's occurrence would necessitate an infinitely extended waiting period. This is because even the smallest constituent entity, be it a particle, string, or wave, would need an indeterminately long time to influence larger physical scales, thereby instigating any event.

**Non-existence of a smallest particle:** The assertion that the universe is perpetually reducible inevitably leads to the conclusion that there is no smallest, indivisible particle, or unit.

**Existence of a fundamental level:** Therefore, it logically follows that the universe must possess a fundamental level of existence, a point beyond which reduction is unattainable, imposing an inherent limit on the divisibility of the cosmos.

**The fundamental level's shape:** This fundamental level of existence must also possess a specific shape or geometry.

**Void less fundamental structure:** The shape of this fundamental level must exhibit the property of gap-less ness. In other words, it cannot leave voids or gaps between itself and other fundamental points of existence, whether they are larger or smaller than the shape itself. If it were larger, the principle of perpetual reducibility would be violated, and if it were smaller, it would indicate that the chosen shape is not truly fundamental.

**Irregular shapes contradict fundamental nature:** Irregular shapes are incompatible with the concept of a fundamental level of existence. Irregular shapes inherently comprise both larger and smaller facets, which undermines the notion of a fundamental, non-reducible structure, as explained in the previous point.

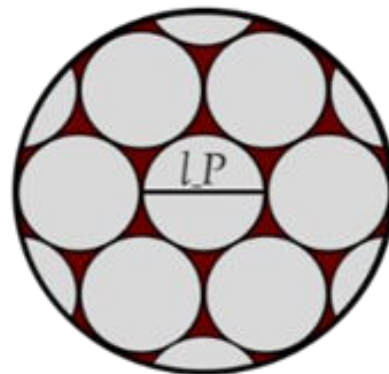
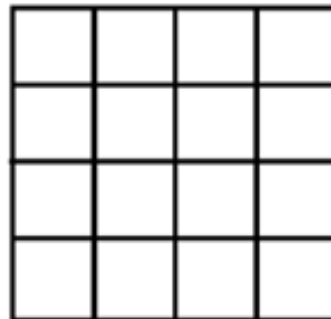
**The necessity of regularity:** Hence, the shape at the fundamental level must be regular. Regular shapes are uniform and do not contain larger or smaller facets, aligning with the concept of a fundamental existence.

**The cube as the ideal shape:** Considering the requirement for a regular, gapless structure, the cube emerges as the most suitable candidate. The cube is the only solid shape that possesses these characteristics, as it can be stacked infinitely without leaving voids, regardless of the number of cubes stacked.

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**The problem with spherical fundamental structures:** If the universe's smallest structure is a sphere, a critical issue arises - the presence of gaps. Despite these gaps being smaller than the spheres themselves, they still have volume. This lack of true gap less ness leads to an infinite reduction process, creating a hierarchy of sizes within the universe. This challenges the idea of an indivisible unit. Hence, alternatives like the cube, with its uniformity and gapless arrangement, offer a more fitting solution to the problem of perpetual reducibility.

## Relations between the Planck scale and the Hubble scale

$$r_H^2 \cdot M_H \cdot t_P^2 \cdot c^2 = m_P \cdot l_P \cdot V_H$$

..

$$V_H \cdot m_P \cdot t_P^2 = M_H \cdot t_H^2 \cdot l_P^3$$

..

$$\hbar_{Max} \cdot l_P \cdot t_P = \hbar \cdot R_H \cdot t_H$$

..

$$m_P \cdot t_P = l_P^2 \cdot R_H \cdot \rho_H \cdot t_H$$

..

$$t_H^3 \cdot m_P \cdot l_P^2 = r_H^5 \cdot \rho_H \cdot t_P^3$$

..

$$l_P = G \cdot \rho_H \cdot r_H \cdot t_H \cdot t_P$$

..

$$m_P^2 \cdot l_P^2 \cdot G = t_P^2 \cdot \hbar \cdot c^3$$

..

$$l_P^2 = G \cdot c^2 \cdot t_H^2 \cdot \rho_H \cdot t_P^2$$

..

$$t_P^2 \cdot r_H^2 \cdot c^3 = \hbar \cdot G \cdot t_H^2$$

..

$$t_P \cdot r_H^3 \cdot \rho_H = m_P \cdot t_H$$

..

$$G \cdot m_P \cdot l_P = c^4 \cdot t_P^2$$

..

$$M_H \cdot l_P = m_P \cdot R_H$$

..

$$M_H \cdot t_P = m_P \cdot t_H$$

..

$$l_P \cdot t_H = t_P \cdot r_H$$

## Results and Discussion

To test variation in the gravitational constant, I suggest the following simple experiments:

**The torsion balance experiment:** The torsion balance experiment could be designed to investigate small changes in the gravitational force. This experiment is formulated with the intent of providing methodology that can be implemented to validate this hypothesis.

**Experimental setup:** The experiment employs a Torsion Balance apparatus, which consists of a horizontal bar suspended from a very thin and delicate torsion wire or fiber. Thinner wires are more sensitive to small forces and can detect subtle changes in gravitational force. At each end of the bar, large masses are affixed. Larger masses will result in more significant twists for the same gravitational force, making variations easier to detect. This balance is placed within a controlled environment to minimize external disturbances, such as air currents and vibrations.

## Experimental procedure

**Calibration:** Before commencing data collection, the Torsion Balance apparatus is carefully calibrated to establish a baseline measurement of the twist angle corresponding to the known, current value of G.

**Environmental control:** The experimental setup is placed in a controlled environment to mitigate external influences. Temperature, humidity, and air currents are carefully regulated.

**Data collection:** Over the course of the experiment, continuous measurements of the twist angle are recorded with high precision. These measurements are taken at regular intervals and span an extended period.

**Data analysis:** The collected data is subjected to rigorous analysis. Statistical methods are applied to assess the significance of any observed variations in the twist angle. Special attention should be given to identifying trends and patterns in the data.

## Key considerations

**Control experiments:** Control experiments are conducted to account for potential sources of experimental error and external influences. These controls may involve altering environmental conditions or introducing known masses to validate the apparatus's sensitivity.

**Data validation:** To ensure data integrity, data validation procedures are implemented, including the identification and elimination of outliers or data artifacts.

**Long-term monitoring:** The experiment extends over an extended duration to increase the statistical significance of any observed variations. Long-term monitoring is essential for detecting gradual changes in  $G$ .

**Remote monitoring:** To minimize human interference and enable continuous data collection, remote monitoring and data transmission capabilities have to be incorporated. This feature facilitates uninterrupted data acquisition over extended durations.

### Simple pendulum experiment

$$f = \frac{1}{2 \cdot \pi} \cdot \sqrt{\frac{g}{L}}, \quad g = \frac{G \cdot M_{Earth}}{R_{Earth}^2}, \quad f = \frac{1}{2 \cdot \pi} \cdot \sqrt{\frac{M_{Earth}}{L(R_{Earth}^2 \cdot \rho_H \cdot t_H^2)}}$$

**Measurement principle:** The experiment leverages the principles of pendulum motion and gravity. Variations in  $G$  could potentially influence the frequency of the oscillation over time.

**Pendulum setup:** One end of the string is attached to the heavy weight, and the other end is secured to a stable support structure, such as a hook or a ceiling anchor. The length of the string remains consistent throughout the experiment.

**Initial measurement:** The length of the pendulum is measured accurately, and this initial length is recorded.

**Vacuum chamber setup:** The entire pendulum apparatus, including the weight and string, is placed inside the vacuum chamber.

**Evacuation of air:** The vacuum chamber is used to remove air from the environment, creating a near-perfect vacuum inside the chamber. This step eliminates air resistance, allowing the pendulum to swing without interference.

**Pendulum swing:** The weight is slightly displaced to one side and released to initiate the pendulum's motion. It swings freely back and forth within the vacuum chamber.

**Time measurement:** A stopwatch or timer is used to measure the time it takes for the pendulum to complete one full oscillation.

**Data recording:** The time taken for the pendulum to complete each oscillation is recorded. The experiment is repeated multiple times to ensure accuracy.

**Extended observations:** Over an extended period, the experiment is periodically repeated within the vacuum chamber, and the time taken for the pendulum to complete one oscillation is recorded.

**Analysis:** The inclusion of a vacuum chamber in the simple pendulum experiment serves to eliminate air resistance, enhancing the accuracy of the experiment. This improved setup still provides a basic exploration of gravity's changes over time. Since gravity is weakening over time, the period of the pendulum will gradually increase.

If a consistent and gradual increase in the pendulum's period is observed over an extended period within the vacuum chamber, it suggests a weakening of gravity. However, this experiment, even with the vacuum chamber, offers a simplified and indirect way to assess this phenomenon.

## Key considerations

While the vacuum chamber eliminates air resistance, other factors such as temperature fluctuations, vibrations, and equipment stability could still affect the pendulum's period. This experiment provides a basic introduction to weakening gravity. For more precise assessments of variations in  $G$ , sophisticated experiments and instruments are required.

## Conclusion

There exists a profound interrelationship between the gravitational constant ( $G$ ), the age of the universe (Hubble time), and density (Hubble density).

Likewise, the speed of light ( $c$ ) is intricately tied to the gravitational constant, density, and the area of the observable universe. The speed of light remains invariably constant, specifically within the Planck and Hubble scales.

The unification equation postulates a profound connection among fundamental constants, including the gravitational constant, vacuum permittivity, and vacuum permeability. It is crucial to note that this equation does not propose a merger of the four fundamental forces of nature but underscores a profound connection among fundamental constants. Beyond offering a fresh perspective on the Law of Universal Gravitation, Coulomb's law for electrostatic force, Coulomb's law of magnetism, and the ratio between these forces, its practical applicability is limited.

The variable constant of the largest quanta, denoted as  $h_{Max}$ , can be conceptualized as the maximum conceivable quantum unit, which escalates with the universe's expansion and aging.  $h_{Max}$  signifies the ultimate unit of action or energy on a cosmic scale, imposing a fundamental boundary on our capacity to acquire knowledge beyond a particular distance.

The Hubble units are the equivalence of Planck units in the sense that they represent the limits of our current understanding of physics, and they are a set of units of measurement defined exclusively in terms of four universal physical constants, in such a manner that these physical constants take on the numerical value of 1 when expressed in terms of these units.

The majority of fundamental constants in nature, such as the speed of light ( $c$ ), the gravitational constant ( $G$ ), the Boltzmann constant ( $K_B$ ), vacuum permittivity ( $\epsilon_0$ ), and vacuum permeability ( $\mu_0$ ), can be derived from Planck and Hubble units.

The fine structure constant ( $\alpha$ ) can be calculated by multiplying the mass and classical radius of an electron or proton and dividing them by the Planck mass and length, and it can also be determined using  $\hbar_{\text{Max}}$  and the Hubble units.

The gravitational clock equation postulates potential weakening of the gravitational constant ( $G$ ) as the universe ages, under the presumption of constant density. While this remains speculative, it could offer an explanation for phenomena like the early universe's large-scale structure and other observations associated with dark matter Figures 3 and 4.

If the gravitational constant is indeed getting weaker with time, then that would indicate that Planck length and time are both increasing as the universe expands and ages. Planck temperature would decrease, and Planck mass would increase as the universe ages and expands.

The calculation of pressure (energy density) is solely applicable to the Hubble scale (cube) and does not encompass the entire universe's energy density. The calculated pressure can be envisaged as the force exerted by photons on the Hubble cube in all directions.

The Planck force was first proposed by the physicist Max Planck; although it wasn't clear what the meaning or purpose of this force value was, I would propose that this is the maximum force possible for both the Hubble and Planck scales. The new method utilizing the maximum force for verifying the precision and authenticity of values can be a valuable tool for understanding values within and between these two scales.

The wave equation, known as the Newton-Laplace equation, can be employed to compute the speed of light when considering the Hubble cube as a closed system. As the Hubble cube expands, both pressure and density increase proportionally, ensuring the constancy of the speed of light during this expansion.

The Hubble acceleration may indicate that the universe was initially curved in its early stages, subsequently evolving towards a flatter configuration as it expands.

There is profound correlation exists between small and large scales, specifically the Planck and Hubble scales, and their mutual connection are evident.

The Hubble scale does not represent the universe's ultimate scale, just as the Planck scale does not signify the smallest possible scale.

Rather, they serve as markers of our observational limitations in this universe, with nature delineating the boundaries of our ability to perceive and understand phenomena beyond these scales.

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