



The Study of Dimensional Flow of Particles and Calculation of Drag Coefficients under Different Viscosity Fluids

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Abstract

An experimental study was conducted to find the drag coefficient of small spheres of diameter 5.0, 3.45, 5.7, 5.45, and 5.20 mm under ethylene glycol, castor oil, and glycerol. Six liquids with different viscosities and densities are used so as to explore a large range of Reynolds numbers. The tubes are divided into different zones of known length. Different spherical balls of various materials and diameters are taken to observe the drag coefficient. The materials of the spherical balls are made up of glass and steel. The setup also included a stopwatch to determine the time duration of various distance intervals, a measuring scale to measure the distance of the intervals on the cylindrical tubes, a screw gauge to note down the diameters of the various spherical balls, a thermometer to note down the temperature.

Keywords: Drag coefficient, Reynolds number, Fluid flow, Stokes law.

Introduction

While processing fluids via pipes and channels, a friction force shows to be a useful quantity. An analogous factor known as drag coefficient is utilized for immersed solids [1, 2]. It is defined as $CD = (FD/ AP)/ \rho u_o^2/2g$ [3].

Where,

FD is the total drag

u_o is the free stream velocity

AP is the projected area of the particle

Dp is the diameter of the particle

For a sphere, $Ap = (\pi/4) Dp^2$

For particles other than spherical, it is necessary to specify size and geometric form of the object and its orientation with respect to the direction of the flow of the fluid.

For a cylinder so oriented that its axis is perpendicular to the flow, Ap is LDp .

For a cylinder with its axis parallel to the direction of the flow, Ap is $(\pi/4) Dp^2$.

From dimensional analysis, the drag coefficient of a smooth solid in an incompressible fluid depends upon a Reynolds number and necessary shape ratios. For a given shape,

$$C_D = \varphi \times Re_p \quad (1)$$

The movement of a particle through a fluid requires external force acting on the particle.

Three forces act on a particle moving through a fluid:

- The external force
- The buoyant force, which acts parallel with the external force but in opposite direction
- The drag force, which appears whenever there is relative motion between the particle and the fluid and it acts to oppose the motion and acts in direction opposite to that of the fluid.

Consider a particle of mass m moving through a fluid under the action of an external force F_e

U : velocity of the particle relative to the fluid

F_b : Buoyant force on the particle

F_D : drag force

Then the resultant force on the particle is:

$$F_e - F_D - F_B \quad (2)$$

Therefore,

$$m \frac{du}{dt} = F_e - F_D - F_B \quad (3)$$

The external force can be expressed as a product of the mass and the acceleration a_e of the particle from this force

$$F_e = m \times a_e \quad (4)$$

The drag force is given by

$$F_D = \frac{C_D u_o^2 \rho A_p}{2} \quad (5)$$

The buoyant force is, by Archimedes' principle, the product of the mass of the fluid displaced by the particle and the acceleration from the external force and is given by

$$F_B = \frac{m \rho a_g}{\rho_n} \quad (6)$$

Substituting equations 4, 5, 6 in equation 3

$$\frac{du}{dt} = a_g - \frac{\rho a_g}{\rho_p} - \frac{C_D u^2 \rho A_p}{2m} = a_g \frac{\rho_p - \rho}{\rho_p} - \frac{C_D u^2 \rho A_p}{2m} \quad (7)$$

At terminal velocity put $\frac{du}{dt} = 0$ and we get

$$u_t = \left(\frac{2g(\rho_p - \rho)m}{A_p \rho_p C_D \rho} \right)^{0.5} \quad (8)$$

If the particles are spheres of diameter D_p

$$m = \frac{\pi}{6} (D_p^3 \times \rho_p) \quad (9)$$

$$A_p = \frac{\pi}{4} (D_p^2) \quad (10)$$

Using the above two equations in equation (7)

$$u_t = \left(\frac{4g(\rho_p - \rho)D_p}{3C_D \rho} \right)^{0.5} \quad (11)$$

Stokes' law:

At low Reynolds numbers, the drag coefficient varies inversely with Rep and the equations for CD, FD and ut are [3, 4]:

The above equation is a form of Stokes' law, which applies when the particle Reynolds number is less than 1.

$$C_D = \frac{24}{Re_p} \quad (12)$$

$$F_D = 3\pi\mu u_t D_p \quad (13)$$

Thus,

$$u_t = \frac{gD_p^2(\rho_p - \rho)}{18\mu} \quad (14)$$

The above equation is a form of Stokes' law, which applies when the particle Reynolds number is less than 1.

Newton's law:

For $1000 < Rep < 200000$, the drag coefficient is approximately constant, and the equations are

$$C_D = 0.44 \quad (12)$$

$$F_D = 0.055\pi D_p (2u_t) 2\rho \quad (13)$$

Thus,

$$u_t = 1.75 \left(\frac{gD_p(\rho_p - \rho)}{\rho} \right)^{0.5} \quad (15)$$

The above equation is Newton's law and applies only for fairly large particles falling in gases or low viscous fluids.

From the equation given by Turton and Levenspiel:

$$C_D = \frac{24}{N_{Re}} (1 + 0.173 N_{Re}^{0.657}) + \frac{0.413}{1 + \frac{16300}{N_{Re}^{1.09}}} \quad (16)$$

This equation defines the complete solid drag curve for $< 2^*$

Experimental Procedure

The temperature was noted down using a thermometer.

The viscosities and densities of six different liquids taken in cylindrical tubes were noted.

5 spherical balls of different sizes and material were taken and their diameter using screw gauge was noted.

Cylindrical tube was divided into different zones of known length having a static liquid.

A spherical ball of known diameter was dropped into the cylindrical tube, taking care that it does not touch the boundaries by dropping it almost from the middle of the tube.

The time of fall of each ball in each interval was noted carefully with the help of the bulb.

For each ball the reading was taken at least three times to reduce the error.

The same procedure was repeated for the remaining tubes.

Recordings

Density of Glass = 2600 kg/m³

Density of Steel = 7800 kg/m³

Table 1: Properties of fluids.

Fluid	Density (kg/m ³)	Viscosity (kg/m s)
PIPE 1	900	0.2
PIPE 2	911	0.084

Table 2: Specifications of balls used.

Ball	Name	Diameter (mm)
Big steel ball	S1	5
Medium steel ball	S2	3.45
Large Glass ball	G1	5.7
Medium glass ball	G2	5.45
Small glass ball	G3	5.2

Observations

Table 3: Observation table for ethylene glycol.

Ball	t1 (sec)	t2 (sec)	t3 (sec)
	s1 = 0.297m	s2 = 0.316m	s3 = 0.279m
Small Glass Ball	0.88	1.14	1
	0.95	1.13	1.08
	1.14	1.17	1.2
Medium Steel Ball	0.12	0.37	0.61
	0.18	0.2	0.44
	0.18	0.45	0.28
	0.22	0.54	0.36
Small Steel Ball	0.4	0.41	0.16
	0.29	0.39	0.22
	0.2	0.41	0.38
	0.26	0.47	0.28
Large Glass Ball	0.86	1.1	0.72
	0.89	1.14	0.85
	0.73	0.84	0.88
	0.91	0.69	0.63

Table 4: Observation table for castor oil.

Ball	t1	t2	t3
	s1 = 0.297m	s2= 0.316m	s3= 0.279m
Small Glass Ball	20.21	25.49	22.92
	21.59	24.21	22.64
	14.92	15.34	25.11
Medium Steel Ball	4.3	4.52	4.93
	4.46	4.99	6.36
	4.18	4.55	4.65
	4.2	4.32	4.59

Small Steel Ball	6.55	6.58	6.8
	6.43	6.63	6.07
	6.44	7.06	11.38
	6.43	6.7	7.26
Large Glass Ball	17.58	17.81	19.1
	17.36	18.8	20.8
	14.7	15.09	15.83
	20.71	22.54	23.68

Table 5: Observation table for glycerol.

Ball	t1	t2	t3
	s1 = 0.297m	s2= 0.316m	s3= 0.279m
Small Glass Ball	7.23	6.69	7.49
	6.78	7.23	8.45
	6.82	7.29	8.72
Medium Steel Ball	1.38	1.58	1.48
	1.41	1.45	1.69
	1.54	1.32	1.85
Small Steel Ball	1.98	2.07	2.49
	1.79	2.08	2.48
	1.83	2.16	2.46
	4.22	5.03	5.47
Large Glass Ball	3.99	4.34	4.93
	4.95	5.22	5.97

Calculations

Table 6: Calculations for ethylene glycol.

Ball	t1	t2	t3	v1	v2	v3	v average	Exp. Terminal Velocity	Re	Theo. Terminal Velocity	CD, experimental	CD, theoretical
	s1 = 0.297m	s2 = 0.316m	s3 = 0.279m									
Small Glass Ball	0.88	1.14	1	0.3375	0.277193	0.279	0.297898	0.278602	6.740951	0.06166	3.5603286	5.7183054
	0.95	1.13	1.08	0.3126316	0.279646	0.258333	0.283537					
	1.14	1.17	1.2	0.2605263	0.270085	0.2325	0.254371					
Medium Steel Ball	0.12	0.37	0.61	2.475	0.854054	0.457377	1.262144	1.142446	31.90704	0.36946	0.7521851	2.0192587
	0.18	0.2	0.44	1.65	1.58	0.634091	1.28803					

	0.18	0.45	0.28	1.65	0.70 2222	0.99 6429	1.11 6217					
	0.22	0.54	0.36	1.35	0.58 5185	0.77 5	0.90 3395					
Small Steel Ball	0.4	0.41	0.16	0.74 25	0.77 0732	1.74 375	1.08 5661	1.01 3381	22.4 1776	0.23 179	1.07 05798	2.50 02378
	0.29	0.39	0.22	1.02 41379	0.81 0256	1.26 8182	1.03 4192					
	0.2	0.41	0.38	1.48 5	0.77 0732	0.73 4211	0.99 6647					
	0.26	0.47	0.28	1.14 23077	0.67 234	0.99 6429	0.93 7026					
Large Glass Ball	0.86	1.1	0.72	0.34 53488	0.28 7273	0.38 75	0.34 0041	0.35 7212	10.6 6791	0.09 394	2.24 97388	4.09 35011
	0.89	1.14	0.85	0.33 37079	0.27 7193	0.32 8235	0.31 3045					
	0.73	0.84	0.88	0.40 68493	0.37 619	0.31 7045	0.36 6695					
	0.91	0.69	0.63	0.32 63736	0.45 7971	0.44 2857	0.40 9067					

Table 7: Calculations for castor oil.

Calculations for glycerol.

Ball	t1	t2	t3	v1	v2	v3	v average	Exp. U	Re	Theo. U	CD, experimental	CD, theoretical
	s1 = 0.297m	s2= 0.316m	s3= 0.279m									
Small Glass Ball	20.21	25.49	22.92	0.01469 57	0.01239 7	0.01217 3	0.01308 8	0.01444 61	0.08377 5	0.01886 6	286.482 44	296.201 62
	21.59	24.21	22.64	0.01375 64	0.01305 2	0.01232 3	0.01304 4					
	14.92	15.34	25.11	0.01990 62	0.0206	0.01111 1	0.01720 6					
Medium Steel Ball	4.3	4.52	4.93	0.06906 98	0.06991 2	0.05659 2	0.06519 1	0.06454 25	0.37429 1	0.10488 8	64.1212 56	69.9375 62
	4.46	4.99	6.36	0.06659 19	0.06332 7	0.04386 8	0.05792 9					
	4.18	4.55	4.65	0.07105 26	0.06945 1	0.06	0.06683 4					
	4.2	4.32	4.59	0.07071 43	0.07314 8	0.06078 4	0.06821 6					
Small Steel Ball	6.55	6.58	6.8	0.04534 35	0.04802 4	0.04102 9	0.04479 9	0.04344 92	0.25196 8	0.06580 5	95.2502 17	101.912 09
	6.43	6.63	6.07	0.04618 97	0.04766 2	0.04596 4	0.04660 5					
	6.44	7.06	11.38	0.04611 8	0.04475 9	0.02451 7	0.03846 5					
	6.43	6.7	7.26	0.04618 97	0.04716 4	0.03843	0.04392 8					
Large Glass Ball	17.58	17.81	19.1	0.01689 42	0.01774 3	0.01460 7	0.01641 5	0.01629 06	0.09447 1	0.02874 2	254.045 28	263.372 01
	17.36	18.8	20.8	0.01710 83	0.01680 9	0.01341 3	0.01577 7					
	14.7	15.09	15.83	0.02020 41	0.02094 1	0.01762 5	0.01959					
	20.71	22.54	23.68	0.01434 09	0.01402	0.01178 2	0.01338 1					

Results

Figure 1: Plot of CD experimental versus CD theoretical.

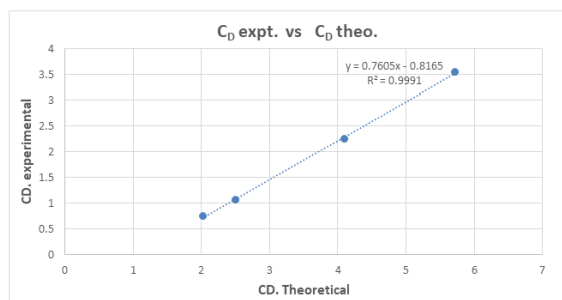


Figure 2: Plot of CD experimental versus Reynolds number.

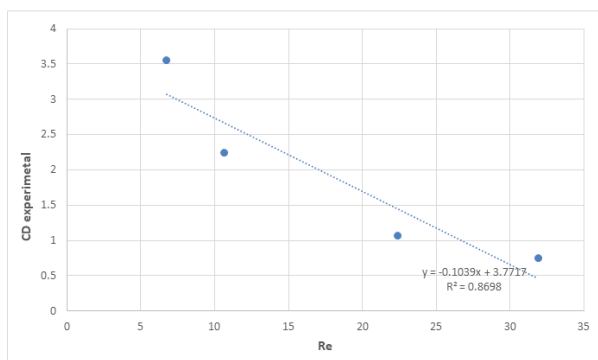


Figure 3: Plot of U theoretical versus U experimental.

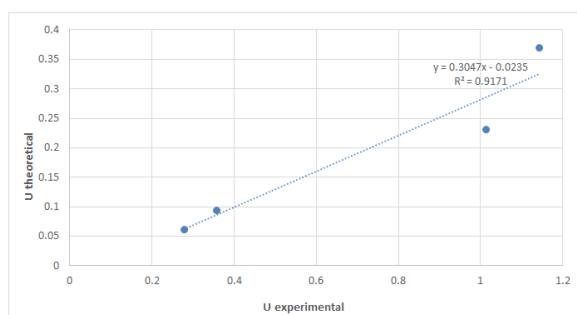


Figure 4: Plot of CD experimental versus CD theoretical.

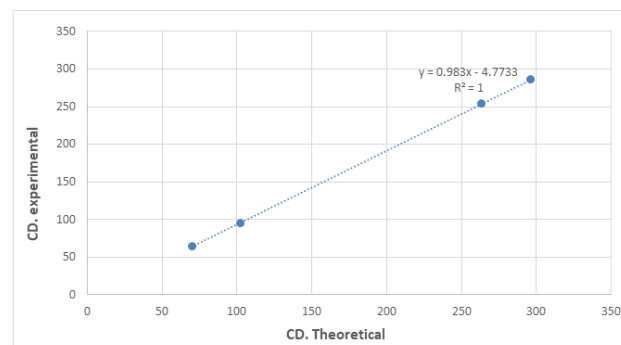


Figure 5: Plot of CD experimental versus Reynolds number.

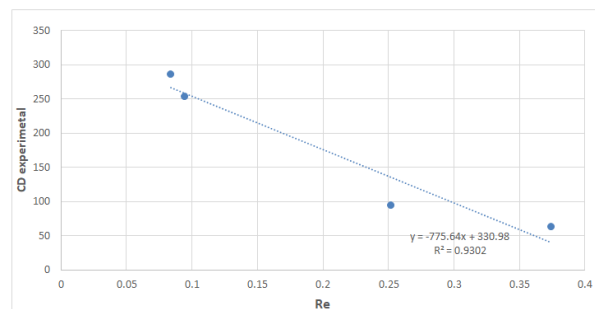


Figure 6: Plot of U theoretical versus U experimental.

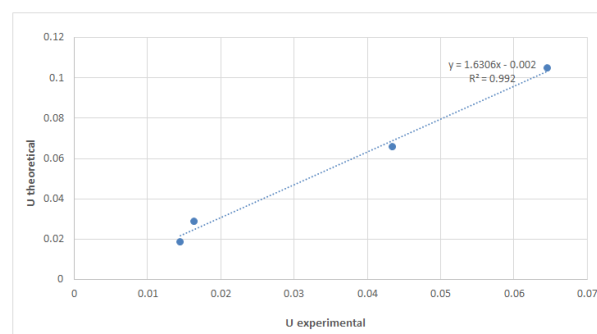


Figure 7: Plot of CD experimental versus CD theoretical.

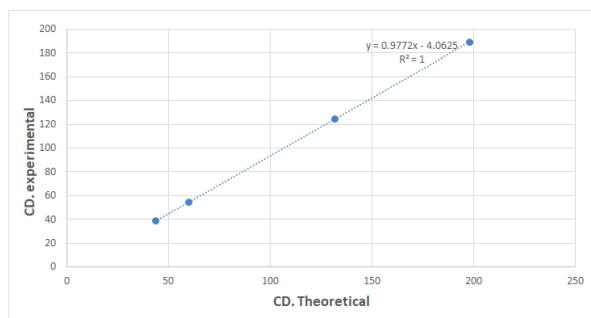


Figure 8: Plot of CD experimental versus Reynolds number.

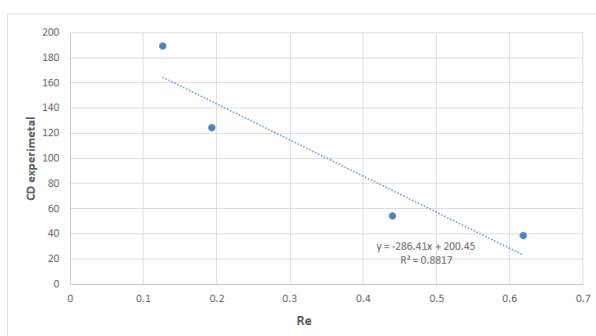
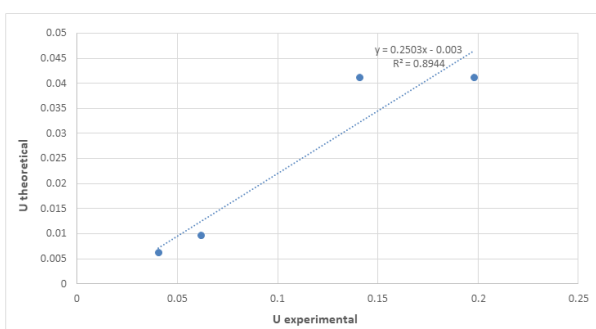


Figure 9: Plot of U theoretical versus U experimental.



Discussion of Result

From the experiment we studied the nature of different fluids of different densities and viscosities. We saw the variation in drag coefficient by varying the Reynolds No. i.e. we used spherical balls of various materials as well as diameters. We saw there were quite discrepancies in the experimental and the theoretical plot of velocity and coefficient of drag vs Reynolds no. The discrepancies may be due to parallax, error in noting the time, wall effects, instrumental error due to screw gauge in measuring the diameter and human error might also have crept in due a large no. of people working at the same time.

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