Supercontinuum Generation Using Microstructured Optical Fibers

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Abstract
The supercontinuum generation results generally from the synergy between several fundamental nonlinear processes, such as self-phase modulation, cross-phase modulation, stimulated Raman scattering, and four-wave mixing. The relative importance of these processes depends on the spectral location and power of the pump, as well as the nonlinear and dispersive characteristics of the medium. Several types of microstructured optical fibers with optimized designs, have been developed during the recent years in order to enhance the supercontinuum generation. This paper provides an overview of the peculiar dispersive and nonlinear properties exhibited by these fibers, including the supercontinuum generation by femtosecond pumping.

Keywords
Optical fibers; Supercontinuum generation; Raman scattering

Introduction
A number of third order nonlinear processes can occur when high-power light is launched into the optical fibers [1]. These can grow to appreciable magnitudes over the long lengths available in fibers, even though the nonlinear index of the silica glass is very small (n_2 = 2.35x10^-20 m^2/W) at 1550 nm [2].

Fiber nonlinearities fall into two general categories [1]. The first category arises from modulation of the refractive index of silica by intensity changes in the signal (Kerr effect). This gives rise to nonlinearities such as self-phase modulation (SPM) [3], cross-phase modulation (XPM) [4], four-wave mixing (FWM) [5], and modulation instability (MI). The second category of nonlinearities corresponds to stimulated scattering processes, such as stimulated Brillouin scattering (SBS) [6] and stimulated Raman scattering (SRS) [7], which are interactions between optical signals and acoustic or molecular vibrations in the fiber, respectively.

A rather interesting nonlinear phenomenon which can be observed in optical fibers is the supercontinuum generation (SCG), which corresponds to an extremely wide spectrum, achieved by an optical pulse along its propagation [8]. It results generally from the synergy between several fundamental nonlinear processes, such as SPM, XPM, SRS, MI, and FWM [1]. The spectral locations and powers of the pumps, as well as the nonlinear and dispersive characteristics of the fiber determine the relative importance and the interaction between these nonlinear processes. A supercontinuum source can find applications in the area of bio-medical optics, where it allows the improvement of longitudinal resolution in optical coherence tomography (OCT) by more than an order of magnitude [9]; in optical frequency metrology [10]; in all kinds of spectroscopy, and as multiwavelength source in the telecommunications area [11].

The fiber nonlinearity is commonly characterized by the nonlinear parameter γ, which is given by (1)

γ = \frac{2\pi n_2}{\lambda} \frac{A_{eff}}{\lambda} \tag{1}

where λ is the light wavelength, n_2 is the nonlinear-index coefficient of the fiber core and A_{eff} is the effective mode area, given by:

A_{eff} = \frac{\iint |F(x,y)|^2 dx dy}{\iint |F(x,y)|^2 dx dy} \tag{2}

F(x,y) representing the spatial distribution of the fiber mode.

Equation (1) shows that, for a fixed wavelength, since n_2 is determined by the material from which the fiber is made, the most practical way of increasing the nonlinear parameter γ is to reduce the effective mode area A_{eff}. However, the nonlinear parameter γ can also be enhanced using the dopant dependence of the nonlinear refractive index n_2. It has been shown that n_2 increases by doping the bulk glass with GeO_2 [17]. On the other hand, n_2 decreases in the case of an F-doped bulk glass.

Fiber Non-linearity and Dispersion
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Fiber dispersion
The mode-propagation constant β(ω) is related with the refractive index n(ω) in the form

β(ω) = \frac{ωn(ω)}{c} \tag{3}

Mathematically, the effects of fiber dispersion are accounted for by expanding β(ω) in a Taylor series about the carrier frequency ω_0 at which the pulse spectrum is centered:

β(ω) = \beta_0 + \beta_1(ω - ω_0) + \frac{1}{2}\beta_2(ω - ω_0)^2 + ... \tag{4}

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where
\[ \beta_j = \left( \frac{d^2 \beta}{d\omega^2} \right)_{\omega=0} \quad (j = 0, 1, 2, \ldots) \quad (5) \]

The group velocity dispersion (GVD) is characterized by the parameter \( \beta_2 \)
\[ \beta_2 = \frac{d^2 \beta}{d\omega^2} = -\frac{d\nu_0}{d\omega} \frac{v_p^2}{c} \quad (6) \]

where \( \nu_0 = \omega / c \) and \( v_p = n_0+\omega (dn/d\omega) \) represent the group velocity and the group refractive index, respectively. In practice, the GVD is often characterized by another parameter, \( D \), given by
\[ D = \frac{2\pi c \beta_2}{\lambda} = -\frac{\lambda}{c} \frac{dn}{d\lambda} \]

The parameter \( D \) gives the delay of arrival time in ps unit for two wavelength components separated by 1 nm over a distance of 1 km. In the case of fused silica, \( D = 0 \) at \( \lambda = 1.276 \mu \text{m} \), which is referred to as the silica zero-dispersion wavelength. The parameter \( D \) becomes negative (normal GVD) at shorter wavelengths and positive (anomalous GVD) at longer wavelengths.

The overall GVD of a guided mode in an optical fiber depends not only on the material dispersion, but also on the waveguide dispersion [1]. The last contribution becomes especially important in the case of fibers using a large difference in refractive index between the core and cladding materials. Besides affecting the dispersion characteristics, increasing such refractive index difference provides also an enhancement of the nonlinear parameter of the fiber, as discussed previously.

**Microstructured optical fibers**

Microstructured optical fibers (MOFs) represent a new class of optical fibers that are characterized by the fact that the silica cladding presents an array of embedded air holes. They are also referred as photonic crystal fibers (PCFs), since they were first realized in 1996 in the form of a photonic crystal cladding with a periodic array of air holes [14].

Microstructured fibers can be divided in two main types. One class of fibers, first proposed in 1999 [18], has a central region containing air. Such fibers are usually called hollow-core MOFs and the light propagating in them is confined to the core by the photonic bandgap effect. The nonlinear effects are strongly reduced and the dispersion becomes negligible in this kind of MOFs. A nonlinear coefficient \( \lambda = 240 \text{W}^{-1} / \text{km} \) provides a nonlinear length \( L_{NL} = (\lambda P L)^{-1} \times 1 \text{mm} \). For dispersion values in the range \(-400 < \beta_2 < 400 \text{ps}^2 / \text{km} \) and pulse durations \( T_0 = 300 \text{fs} \), we have a dispersion length \( L_D = T_0^2 / \beta_2 = 0.2 \text{m} \). Considering also typical values of fiber loss \( (\alpha = 1-100 \text{dB/km}) \), we conclude that both the effective fiber length \( L_{eff} = (1-\exp(-\alpha L)) \) and the dispersion length \( L_D \) are much longer than the nonlinear length \( L_{NL} \), which means that strong nonlinear effects will be readily observable in solid-core MOFs.

A peak power of \( P = 5 \text{kW} \) launched into a silica MOF with a nonlinear coefficient \( \lambda = 240 \text{W}^{-1} / \text{km} \) provides a nonlinear length \( L_{NL} = (\lambda P L)^{-1} \times 1 \text{mm} \). For dispersion values in the range \(-400 < \beta_2 < 400 \text{ps}^2 / \text{km} \) and pulse durations \( T_0 = 300 \text{fs} \), we have a dispersion length \( L_D = T_0^2 / \beta_2 = 0.2 \text{m} \). Considering also typical values of fiber loss \( (\alpha = 1-100 \text{dB/km}) \), we conclude that both the effective fiber length \( L_{eff} = (1-\exp(-\alpha L)) \) and the dispersion length \( L_D \) are much longer than the nonlinear length \( L_{NL} \), which means that strong nonlinear effects will be readily observable in solid-core MOFs.

The microstructured cladding offers greatly enhanced design flexibility and can manipulate the dispersion characteristics by controlling structural parameters such as the hair-hole diameter \( d \) and the hole-to-hole spacing \( A \) [25]. In fact, the dispersive properties of MOFs are quite sensitive to these parameters and can be tailored by changing appropriately each of them. Figure 3 shows the dispersion characteristics of a microstructured fiber with a hexagonal pattern of holes spaced by \( a \) for different hole-pitch ratios.

In solid-core MOF, as the holes get larger, the core becomes more and more isolated, until it resembles an isolated strand of silica glass. The core diameter of a MOF is given by \( D_{core} = 2 \pi - d \). MOFs with larger
cores exhibit semi-infinite anomalous dispersion above the ZDW. By decreasing the core size, the ZDW tends to be shifted to a shorter wavelength, leading to the anomalous dispersion at near infrared and visible wavelengths. When the core size is decreased further, a second ZDW arises in the longer wavelength side, such that the GVD is anomalous in the spectral window between the two ZDWs and normal outside it. This situation can be seen in some cases of Figure 3(a), 3(b). Submicron-diameter MOF cores have been fabricated using a conventional tapering process [26].

Modelling of the Supercontinuum

Modelling the supercontinuum generation can be realized considering a generalized NLSE that includes higher-order dispersion effects, as well as intrapulse Raman scattering. Such equation can be written as (1).

$$\frac{\partial U}{\partial z} = \sum_k \beta_k \frac{\partial^2 U}{\partial t^2} + \alpha(\omega) \frac{\partial U}{\partial t} \left[ 1 - \frac{\partial}{\partial \omega} \right] U(z,t) + \left[ \frac{\partial R}{\partial \omega} \right] \left[ \frac{\partial U(z,t)}{\partial t} \right]$$

where $U(z,t)$ is the electric field envelope, $\omega_0$ is the center frequency, $\beta_k$ are the dispersion coefficients at the center frequency, $\alpha(\omega)$ is the frequency-dependent fiber loss, and $\lambda$ is the nonlinear parameter.

The nonlinear response function $R(t)$ in Equation (9) can be written as

$$R(t) = (1 - f_R) \delta(t) + f_R h(t)$$

where the $\delta$ function represents the instantaneous electron response (responsible for the Kerr effect), $h(t)$ represents the delayed ionic response (responsible for the Raman scattering) and $\int R$ is the fractional contribution of the delayed Raman response to the nonlinear polarization, in which a value $f_R = 0.18$ is often assumed [27]. It is common to approximate $h(t)$ in the form [28,29]

$$h(t) = \frac{\tau_1^2 + \tau_2^2}{\tau_1^2 \tau_2^2} \exp\left(-t / \tau_2\right) \sin\left(t / \tau_1\right)$$

where $\tau_1 = f_R \tau_2$ fs and $\tau_2 = 32$ fs. More accurate forms of the response function $h(t)$ have also recently been investigated [30].

Equation (9) can be used to describe the propagation of femtosecond pulses in optical fibers, in both the normal and anomalous...
dispersion regimes. When such pulses have enough power, their spectra undergo extreme broadening. In the anomalous dispersion regime, this process is mainly influenced by the phenomenon of soliton fission, which occurs whenever a higher-order soliton is affected by third- or higher-order dispersion. The soliton order N is given by [1, 28]

\[
N = \sqrt{\frac{L_{nf}}{L_{nl}}}
\]

(12)

where \(L_{nf} = T_0^2 / P_0 \) is the dispersion distance and \(L_{nl} = 1 / \lambda P_0 \) is the nonlinear length.

In the presence of higher-order dispersion, an Nth-order soliton gives origin to N fundamental solitons whose widths and peak powers are given by [31]

\[
T_k = \frac{T_0}{2N + 1 - 2k}, \quad P_k = \frac{(2N + 1 - 2k)^2}{N^2} P_0
\]

(13)

(14)

where \(k = 1 \) to \( N \), where \( N \) is the integer closest to \( N \) when \( N \) is not an integer. Soliton fission occurs generally after propagation distance \(L_{nf} \sim L_{nl}/N\), at which the injected higher-order soliton attains its maximum bandwidth. The fission distance \(L_{nf} \) is a particularly significant parameter in the context higher-order soliton effect compression [32, 33].

Besides higher-order dispersion, another main effect affecting the dynamics of a higher-order soliton fission is the intrapulse Raman scattering (IRS). This phenomenon leads to a continuous downshift of the soliton carrier frequency, an effect known as the soliton self-frequency shift (SSFS) [34]. Such effect was observed for the first time by Mitschke and Mollenauer in 1986 [35]. The origin of SSFS can be understood by noting that for ultrashort solitons the pulse spectrum becomes so broad that the high-frequency components of the pulse can transfer energy through Raman amplification to the low-frequency components of the same pulse. Such an energy transfer appears as a red shift of the soliton spectrum, with shift increasing with distance.

The rate of frequency shift per propagation length is given by [1]

\[
\frac{df}{dz} = -\frac{4t_r}{15\pi T_0^2} \beta \left[\frac{4t_r}{15\pi T_0^2} \beta\right]^2
\]

(15)

where \(t_r = \int \frac{th(t)dt}{\tau_0} \approx 5fs\) is the Raman parameter and \(\beta\) is the soliton peak power. Since the SSFS effect is proportional to \((\beta P_0)^2\), it will be enhanced if short pulses with high peak pulses are propagated in highly nonlinear fibers.

The fission phenomenon can be observed in Figure 4, which shows the temporal and spectral evolution of an optical pulse along a highly nonlinear MOF with hole diameter \(d=1.4\mu m\) and pitch = 1.6 \(\mu m\). In this case, the dispersion curve has only one zero dispersion wavelength, located at 735 nm. We consider a pump in the anomalous dispersion region at 790 nm, where the nonlinear parameter is \(\lambda = 1177W^{-1}km^{-1}\). An input pulse \(U(0,\tau) = \sqrt{P_0sech(\tau/\tau_0)}\) is assumed, where \(P_0=5KW\) and \(\tau_0=28.4fs\), which corresponds to an intensity full width at half maximum (FWHM) of 50 fs. For the assumed parameters, we have \(N=6.02\).

A clear signature of soliton fission is the appearance of a new spectral peak in Figure 4a at \(z = L_{nf}\). The new spectral peak observed corresponds to the so-called nonsoliton radiation (NSR) [36] or Cherenkov radiation [37] which is emitted by the solitons resulting from the fission process in the presence of higher-order dispersion. When the third-order dispersion coefficient \((\beta_3)\), the NSR is emitted at wavelengths shorter than that of the soliton, as observed in Figure 4a. Regarding the time domain, Figure 4b shows that a dispersive wave spreads with propagation and lags behind the main soliton.

Another noticeable feature in Figure 4 is the red-shift of the solitons created by the fission process. As a consequence of the SSFS induced by intrapulse Raman scattering, such solitons separate from each other. Since the SSFS is the largest for the shortest soliton, its spectrum shifts the most toward the red side in Figure 4a. The change of the soliton’s frequency determines a reduction in the soliton’s speed because of dispersion. This deceleration appears as a bending of the soliton trajectory in the time domain, as observed in Figure 4b.

Figure 5 shows the initial and final pulse profiles, both in frequency and time domains. We observe that a nearly uniform supercontinuum is achieved between 500 nm and 1100 nm. These features are particularly important for achieving high performance OCT. In fact, the extreme nonlinear spectral broadening provided...
by SCG permits a high resolution OCT, while the smooth spectral profile avoids the appearance of side-lobes on the axial point spread function.

Conclusion

The peculiar dispersive characteristics of both tapered and microstructured fibers make them particularly suitable to generate the supercontinuum using commercially available pump sources around 1060 nm and 800 nm. Pumping with femtosecond pulses in the anomalous dispersion region of the fiber, the soliton fission process gives origin to multiple fundamental solitons of different widths and peak powers. Among the host of soliton related effects, there are two which become then particularly important: the SSFS induced by the Raman scattering and the emission of dispersive radiation. Solitons dominate the long-wavelength edge of the supercontinuum, while the dispersive radiation determines the short wavelength expansion. As a result, a wide and nearly uniform supercontinuum can be achieved. This is important for several applications, namely in the area of optical coherence tomography.

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