

Appendix – A

Correlation function determination via expansion of fluctuations into the Fourier series

If the averaged value of T is found, we can calculate the related fluctuations: $T'(x, y, z) = T(x, y, z) - \langle T \rangle$.

Let us expand the fluctuation into the Fourier series. We have

$$T' = \sum_{\alpha} \sum_{\beta} \sum_{\gamma} f_{\alpha\beta\gamma} \exp(i\alpha x + i\beta y + i\gamma z) \quad (\text{A.1})$$

$$\alpha = \pi n_x / L_x,$$

$$\beta = \pi n_y / L_y,$$

$$\gamma = \pi n_z / L_z.$$

$$n_x = -N_x, \dots, N_x,$$

$$n_y = -N_y, \dots, N_y,$$

$$n_z = -N_z, \dots, N_z$$

Here, N_x , N_y , and N_z are the chosen number of harmonics for each coordinate. L_x , L_y , and L_z are the maximum values of x , y , and z .

The correlation function $\langle T'T' \rangle$ takes the form

$$\begin{aligned} \langle T'T' \rangle_{x,y,z} &= \\ &= \left(\int_{-L_x}^{L_x} \int_{-L_y}^{L_y} \int_{-L_z}^{L_z} T'(x_1 + x/2, y_1 + y/2, z_1 + z/2) T'(x_1 - x/2, y_1 - y/2, z_1 - z/2) dx_1 dy_1 dz_1 \right) \times \quad (\text{A.3}) \\ &\times \left(\frac{1}{2L_x} \frac{1}{2L_y} \frac{1}{2L_z} \right) \end{aligned}$$

Another representation of (A.1) is as follows

$$\begin{aligned}
T' = & \left(\frac{a_{0x}}{2} + \sum_{\alpha>0} \frac{a_{\alpha x} - ib_{\alpha x}}{2} \exp(i\alpha x) + \sum_{\alpha<0} \frac{a_{\alpha x} + ib_{\alpha x}}{2} \exp(-i\alpha x) \right) \times \\
& \left(\frac{a_{0y}}{2} + \sum_{\beta>0} \frac{a_{\beta y} - ib_{\beta y}}{2} \exp(i\beta y) + \sum_{\beta<0} \frac{a_{\beta y} + ib_{\beta y}}{2} \exp(-i\beta y) \right) \times \\
& \times \left(\frac{a_{0z}}{2} + \sum_{\gamma>0} \frac{a_{\gamma z} - ib_{\gamma z}}{2} \exp(i\gamma z) + \sum_{\gamma<0} \frac{a_{\gamma z} + ib_{\gamma z}}{2} \exp(-i\gamma z) \right)
\end{aligned} \tag{A.4}$$

Expression (A.2) can be also written in such a form. In this case, (A.3) contains integrals having the form

$$\int \exp(i\alpha(x_1 - x/2)) \exp(i\bar{\alpha}(x_1 + x/2)) dx_1, \tag{A.5}$$

$$\int \exp(i\alpha(x_1 - x/2)) \exp(-i\bar{\alpha}(x_1 + x/2)) dx_1, \tag{A.6}$$

$$\int \exp(-i\alpha(x_1 - x/2)) \exp(i\bar{\alpha}(x_1 + x/2)) dx_1, \tag{A.7}$$

$$\int \exp(-i\alpha(x_1 - x/2)) * \exp(-i\bar{\alpha}(x_1 + x/2)) dx_1, \tag{A.8}$$

$$\int \exp(i\alpha(x_1 - x/2)) dx_1. \tag{A.9}$$

Integrals of type (A.5), (A.8), and (A.9) are zero. This is also the case for integrating over y and z . Integrals (A.6)

and (A.7) equal 1 at $\alpha = \bar{\alpha}$ and 0 for other cases.

This means that the expression for correlation function $\langle T'T' \rangle$ has the form

$$\langle T'T' \rangle = \sum_{\alpha} \sum_{\beta} \sum_{\gamma} f_{\alpha\beta\gamma} \varphi_{\alpha\beta\gamma}^* \exp(i\alpha x + i\beta y + i\gamma z), \tag{A.10}$$

Where $\varphi_{\alpha\beta\gamma}^*$ is the complex conjugation to the coefficient $\varphi_{\alpha\beta\gamma}$.

Any correlation function can be found by formula similar to (A.10).